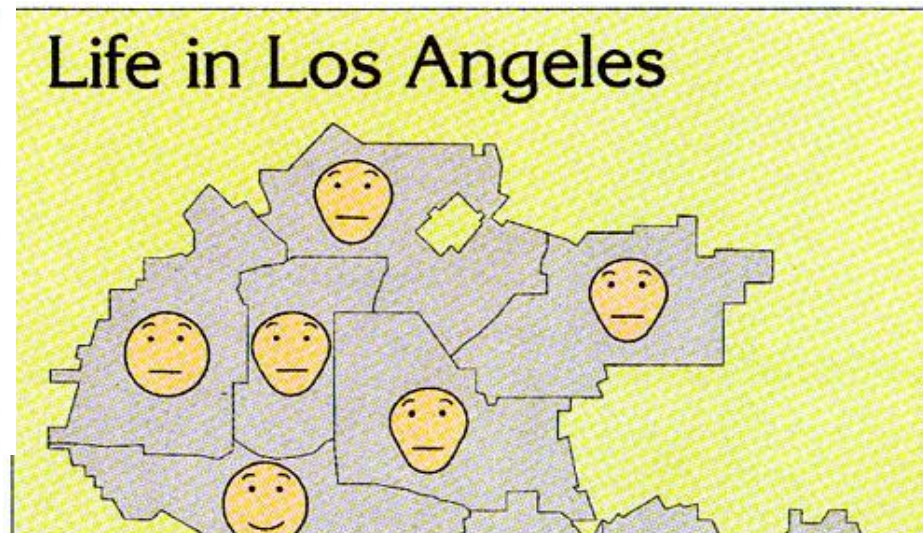
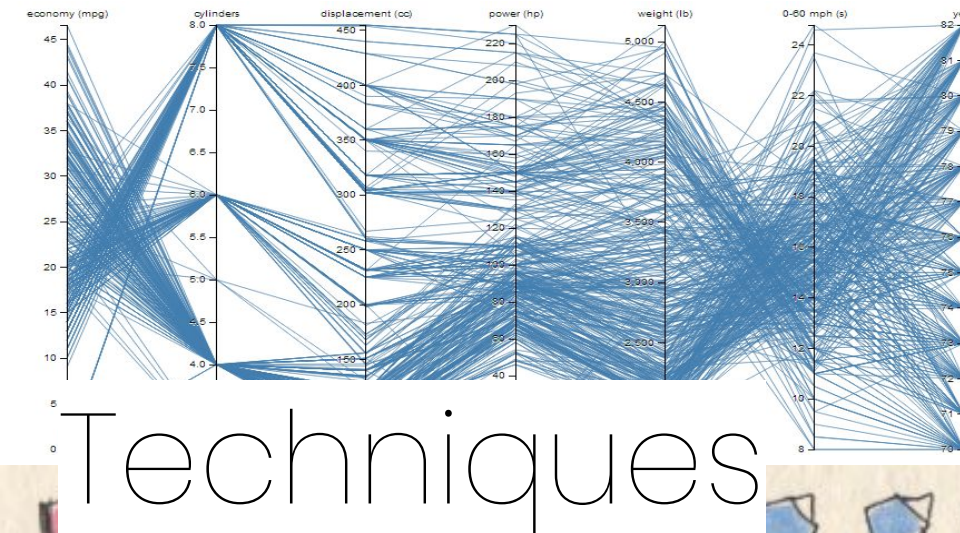
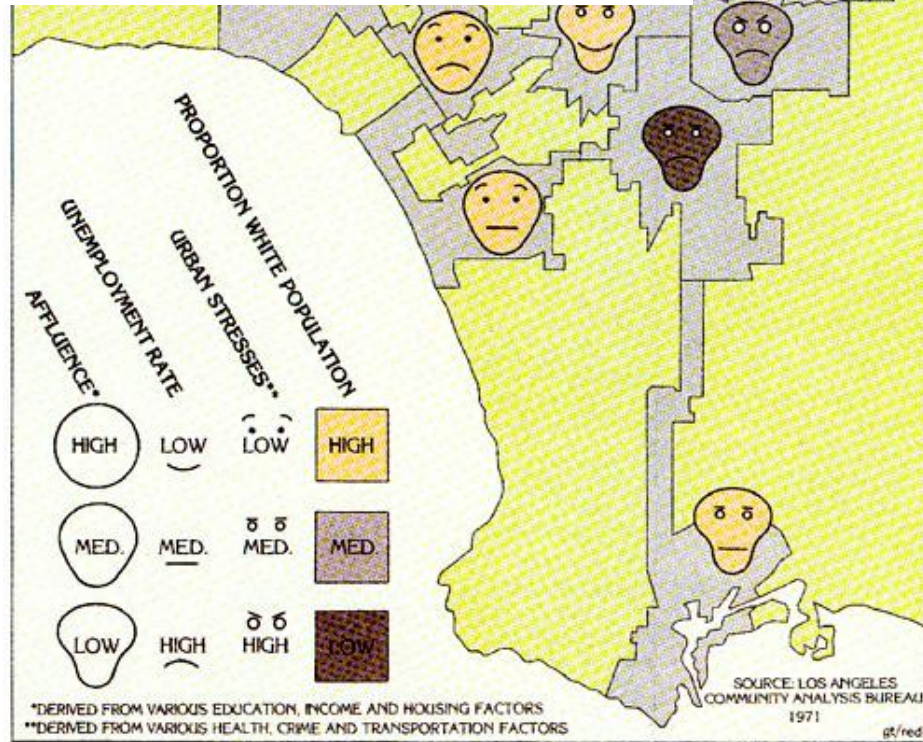




Techniques Multidimensional Data

Benjamin Bach
<http://benjbach.me>
 University of Edinburgh
 2020



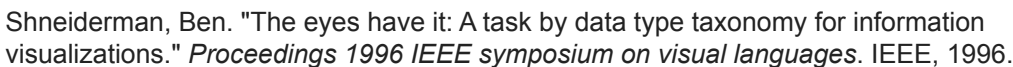
Data Types: Ben Shneiderman

- **1-dimensional**
- 2-dimensional
- 3-dimensional
- Multidimensional
- Temporal
- Trees
- Networks

total_bill
16.99
10.34
21.01
23.68
24.59
25.29
8.77
26.88
15.04
14.78
10.27
35.26

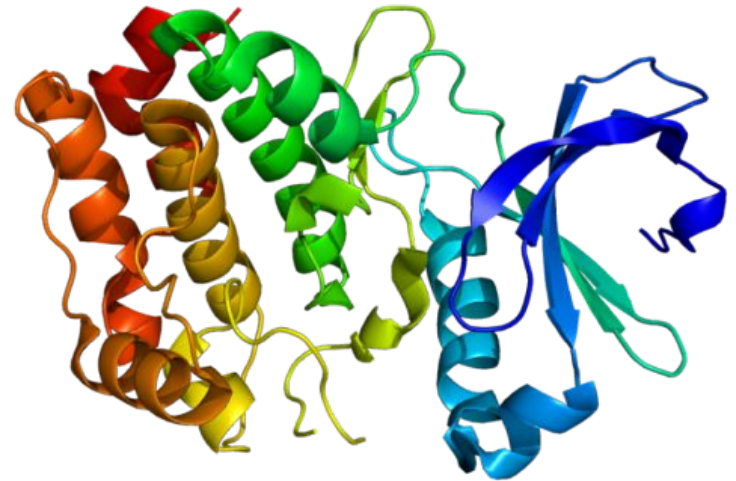
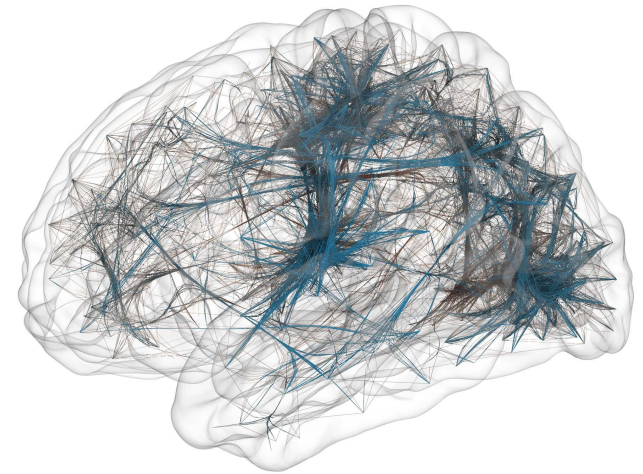
Hr. Anton Joseph Herrenberger.
Hr. Lt. Johann Simon Klein.
Hr. Jacob Galler.
Hr. Lt. Joh. Franz Ehmann.
Hr. Lt. Joh. Friedrich Lauth.
Hr. Franz Placidus Claus.
Hr. Lt. Anton Lepicq.
Hr. Lt. Joh. Christian Treitlinger.
Hr. Lt. Jacob Friedrich Brackenhoffet.
Hr. Lt. Jacob Ludwig Albert.
Hr. Lt. Augustin Meinhard Anton
Lachaulle.
Hr. Joseph Herrmann Duelly.

- 1-dimensional
- **2-dimensional**
- 3-dimensional
- Multidimensional
- Temporal
- Trees
- Networks



Data Types: Ben Shneiderman

- 1-dimensional
- 2-dimensional
- **3-dimensional**
- Multidimensional
- Temporal
- Trees
- Networks



Data Types: Ben Shneiderman

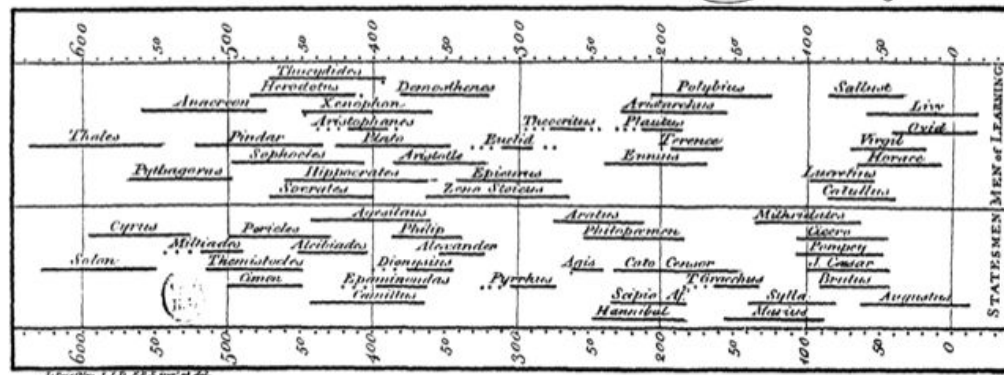
- 1-dimensional
- 2-dimensional
- 3-dimensional
- **Multidimensional**
- Temporal
- Trees
- Networks

total_bill	tip	sex	smoker	day
16.99	1.01	Female	No	Sun
10.34	1.66	Male	No	Sun
21.01	3.5	Male	No	Sun
23.68	3.31	Male	No	Sun
24.59	3.61	Female	Yes	Sun
25.29	4.71	Male	No	Sun
8.77	2	Male	No	Sun
26.88	3.12	Male	No	Sun
15.04	1.96	Male	Yes	Sun
14.78	3.23	Male	Yes	Sun
10.27	1.71	Male	Yes	Sun
35.26	5	Female	No	Sun

Data Types: Ben Shneiderman

- 1-dimensional
- 2-dimensional
- 3-dimensional
- Multidimensional
- **Temporal**
- Trees
- Networks

A Specimen of a Chart of Biography.



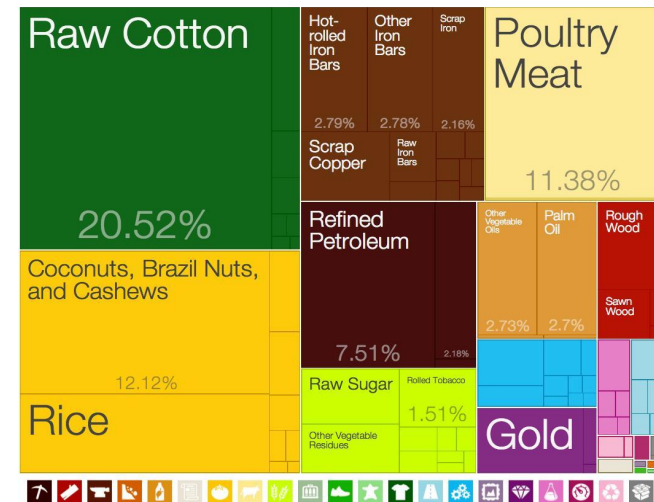
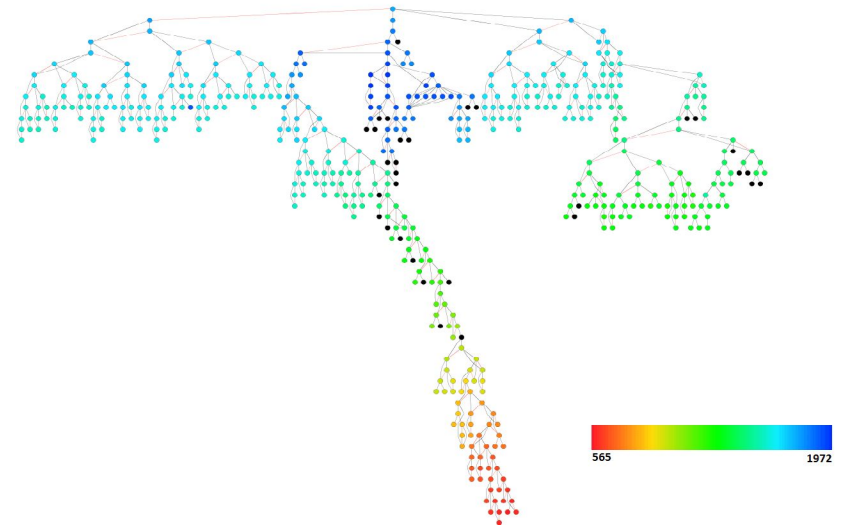
*CHART of all the IMPORTS and EXPORTS to and from ENGLAND
From the Year 1700 to 1800 by R. Playfair*



*The Division at the Bottom, except YEARS, & those on the Right hand, Measures of FORCE
Published in the 5th March 1801, by R. Playfair*

Data Types: Ben Shneiderman

- 1-dimensional
- 2-dimensional
- 3-dimensional
- Multidimensional
- Temporal
- **Trees**
- **Networks**



Data Types: Ben Shneiderman

- 1-dimensional
- 2-dimensional
- 3-dimensional
- Multidimensional
- Temporal
- Trees
- **Networks**

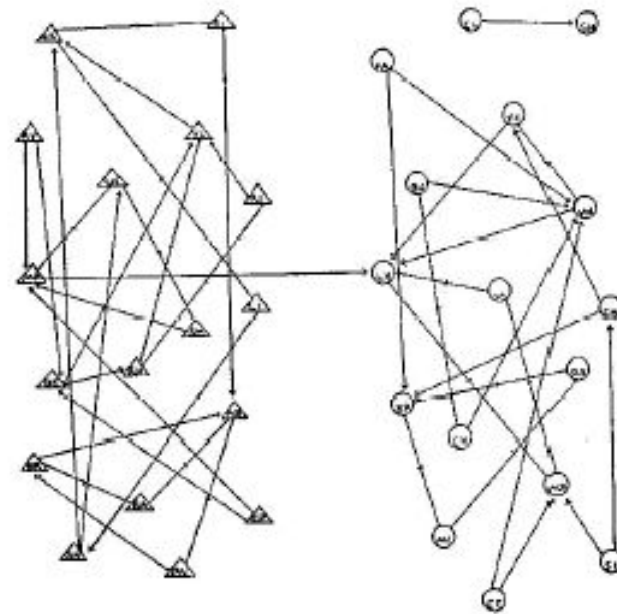
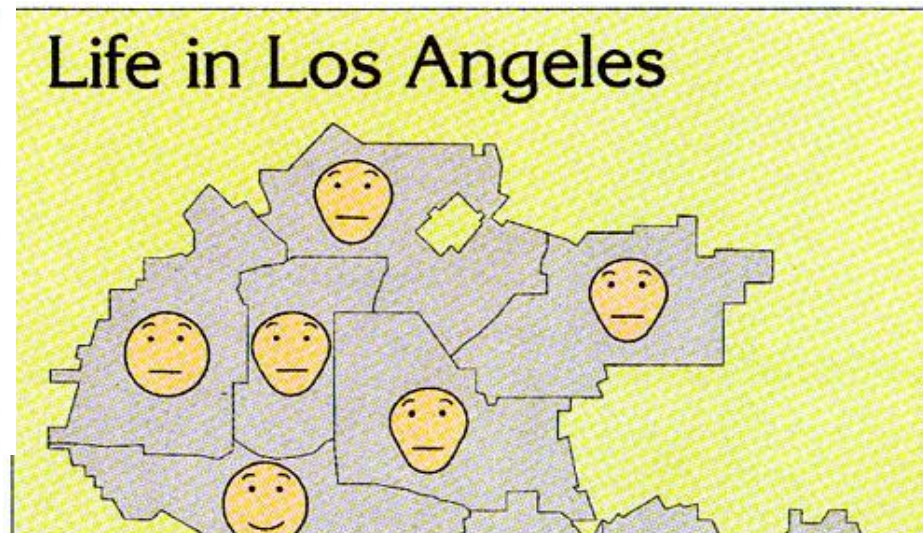
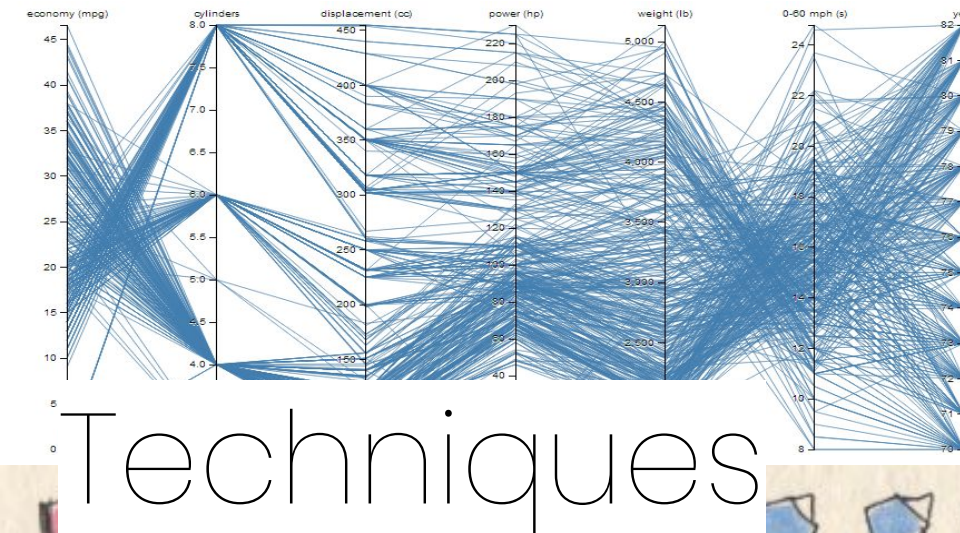
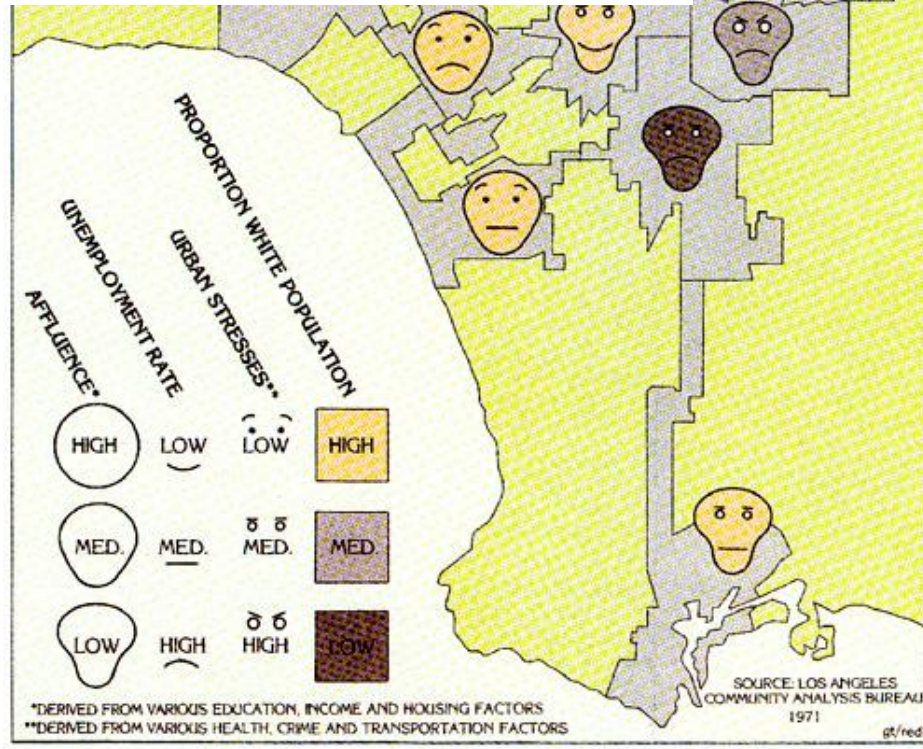


Figure 1. An Attraction Network in a Fourth Grade Class (from Moreno [19], p. 38).



Techniques Multidimensional Data

Benjamin Bach
<http://benjbach.me>
 University of Edinburgh
 2020



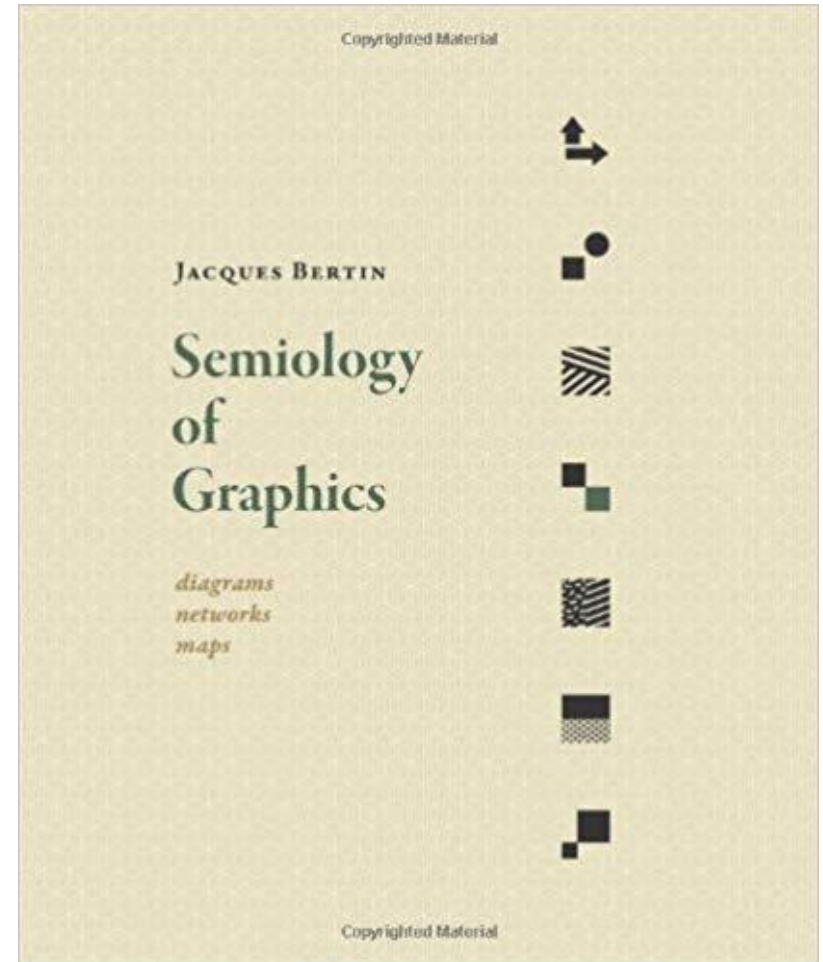
Multidimensional data



total_bill	tip	sex	smoker	day	time	size
16.99	1.01	Female	No	Sun	Dinner	2
10.34	1.66	Male	No	Sun	Dinner	3
21.01	3.5	Male	No	Sun	Dinner	3
23.68	3.31	Male	No	Sun	Dinner	2
24.59	3.61	Female	Yes	Sun	Lunch	4
25.29	4.71	Male	No	Sun	Lunch	4
8.77	2	Male	No	Sun	Dinner	2
26.88	3.12	Male	No	Sun	Dinner	4
15.04	1.96	Male	Yes	Sun	Dinner	2
14.78	3.23	Male	Yes	Sun	Dinner	2
10.27	1.71	Male	Yes	Sun	Dinner	2
35.26	5	Female	No	Sun	Lunch	4

Data types: **Jacques Bertin**

- Quantitative data **Q**
- Ordinal **O**
- Categorical **C**



Multivariate data

Q

Q

C

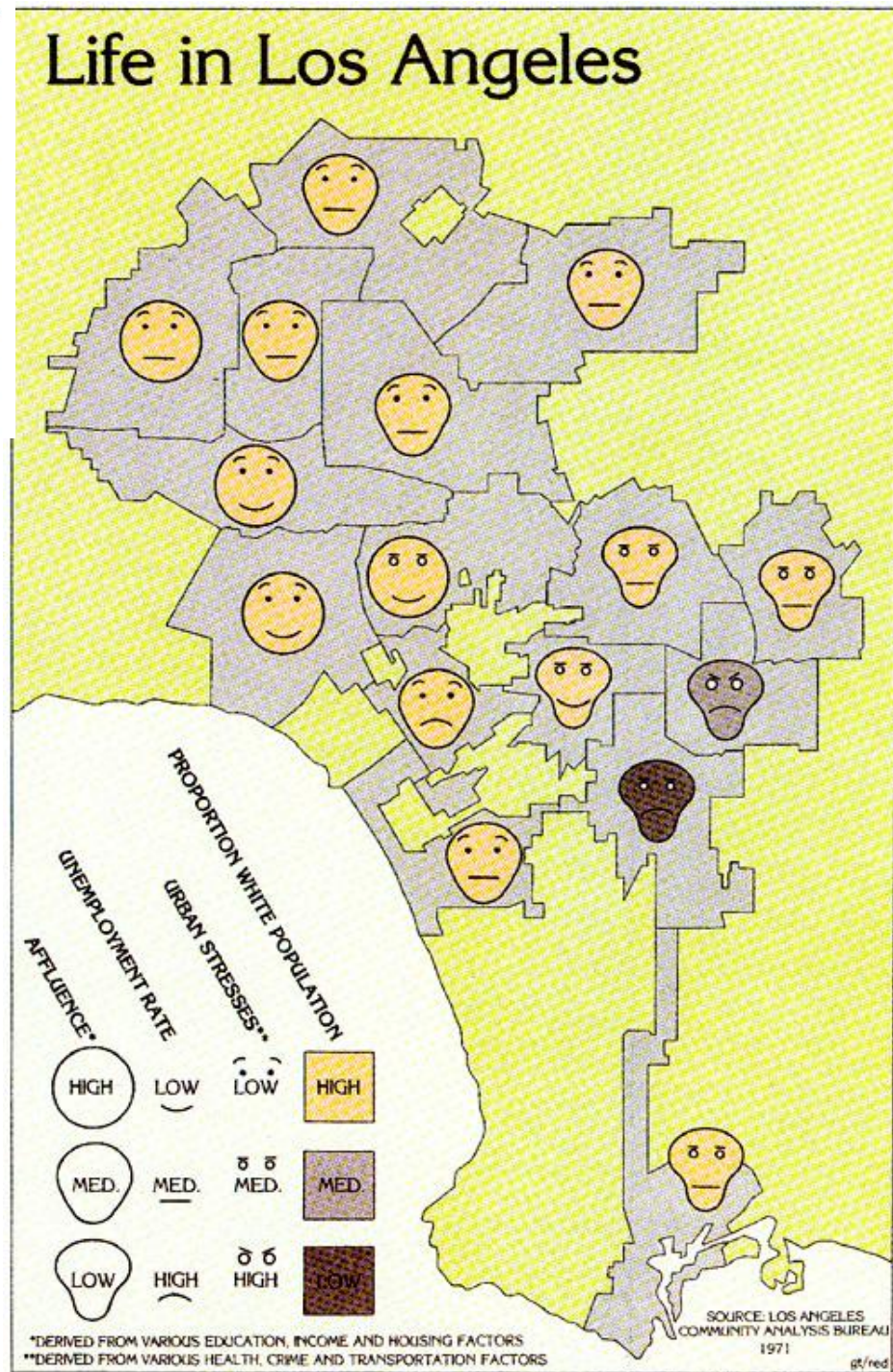
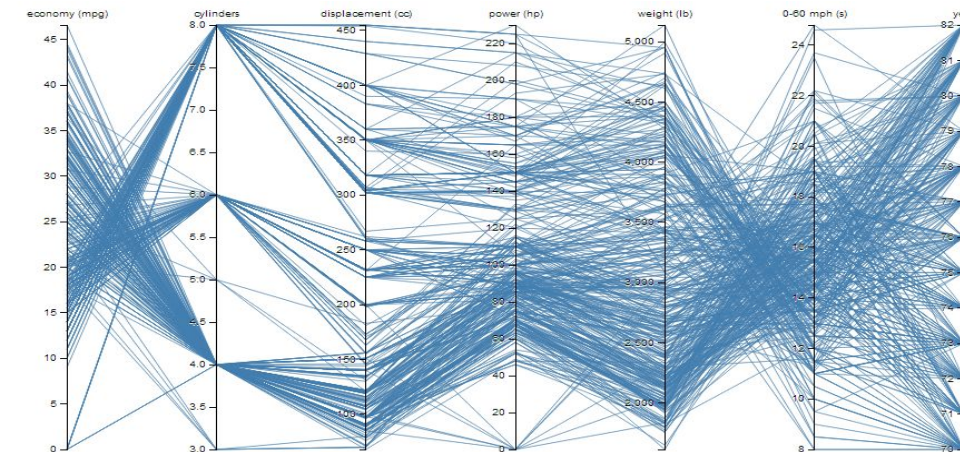
C

Q

O

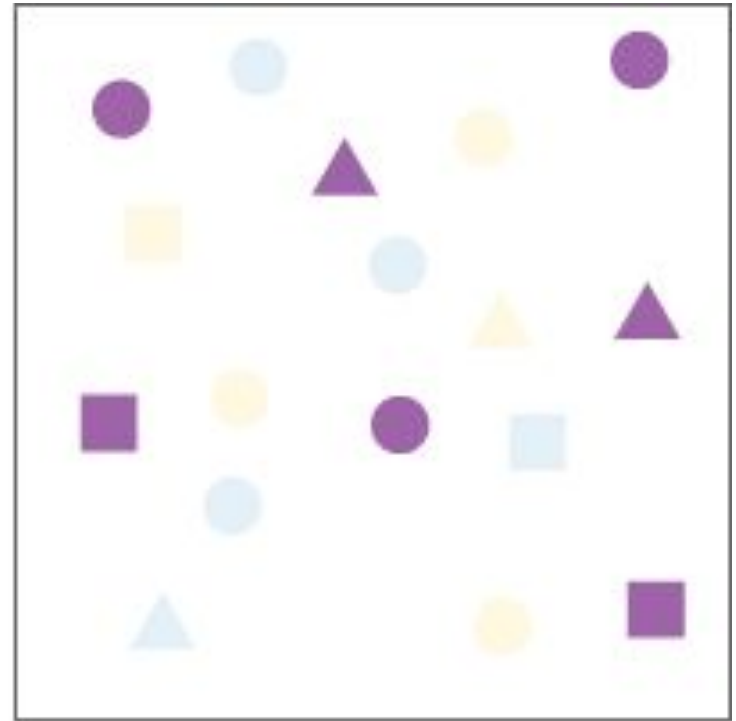
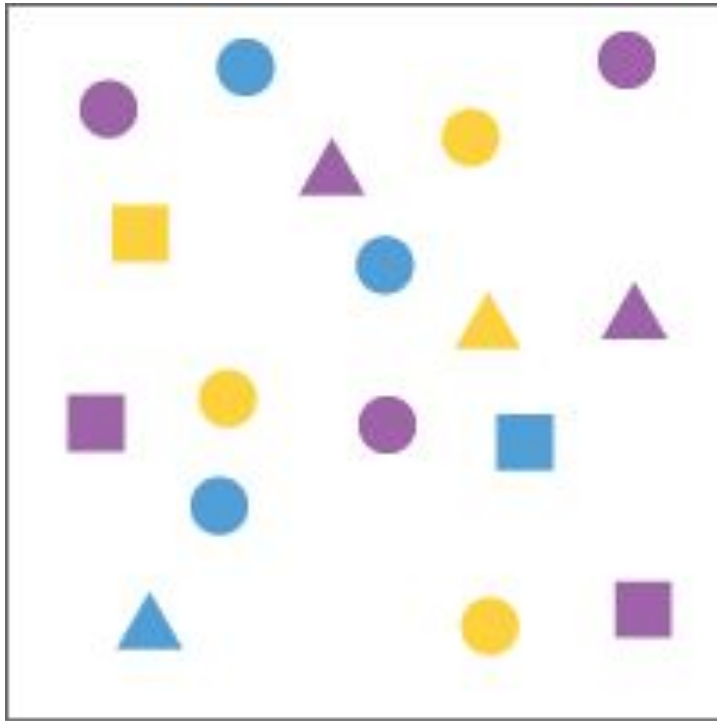
Q

total_bill	tip	sex	smoker	day	time	size
16.99	1.01	Female	No	Sun	Dinner	2
10.34	1.66	Male	No	Sun	Dinner	3
21.01	3.5	Male	No	Sun	Dinner	3
23.68	3.31	Male	No	Sun	Dinner	2
24.59	3.61	Female	Yes	Sun	Lunch	4
25.29	4.71	Male	No	Sun	Lunch	4
8.77	2	Male	No	Sun	Dinner	2
26.88	3.12	Male	No	Sun	Dinner	4
15.04	1.96	Male	Yes	Sun	Dinner	2
14.78	3.23	Male	Yes	Sun	Dinner	2
10.27	1.71	Male	Yes	Sun	Dinner	2
35.26	5	Female	No	Sun	Lunch	4



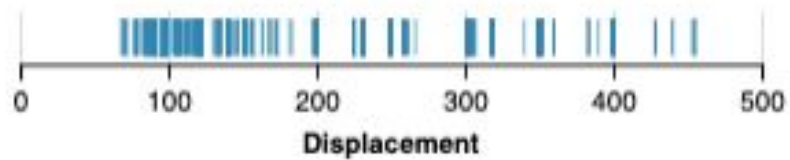
Outline

- Low-dimensions
- Higher dimensions
- Dimensionality reduction

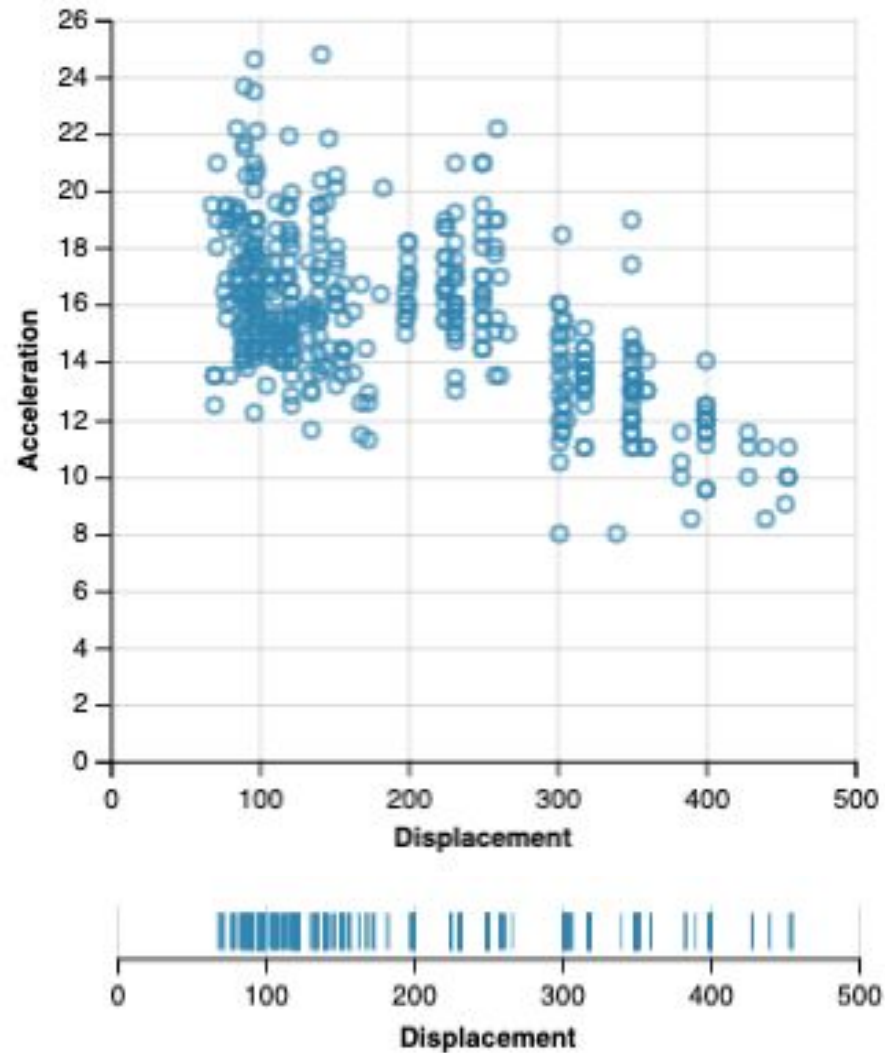


Symbols can be perceived as a group despite variation in shape, e.g., these similarly sized purple symbols appear as a group. Shape is therefore *associative*.

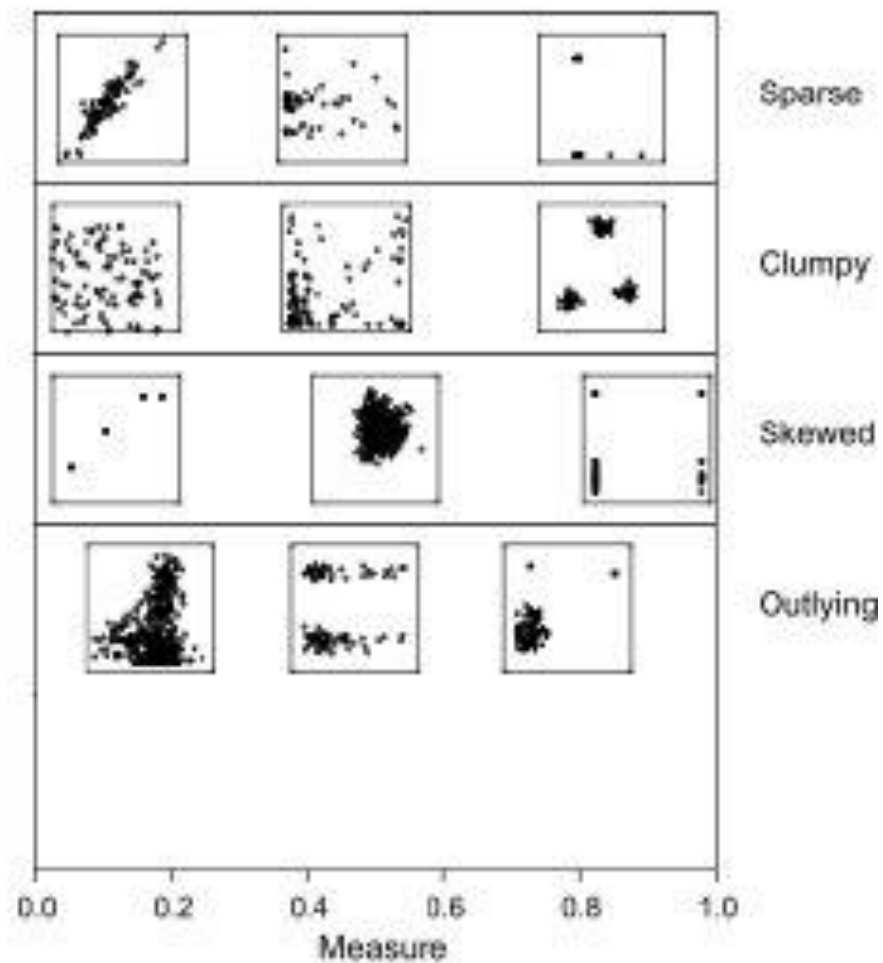
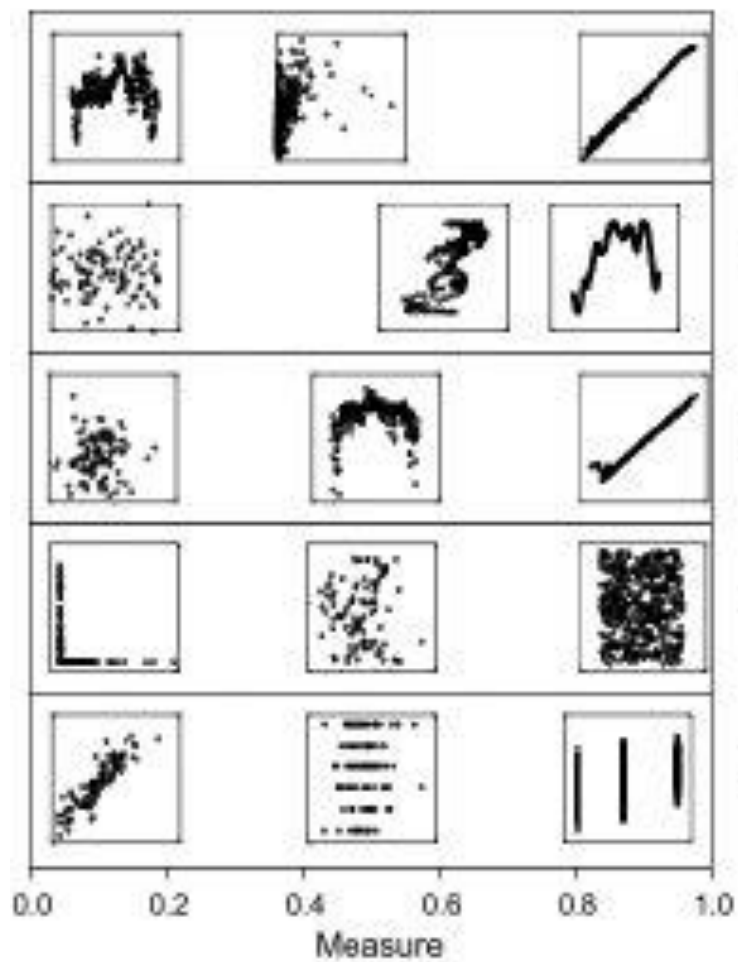
1 Dimension



2 Dimensions

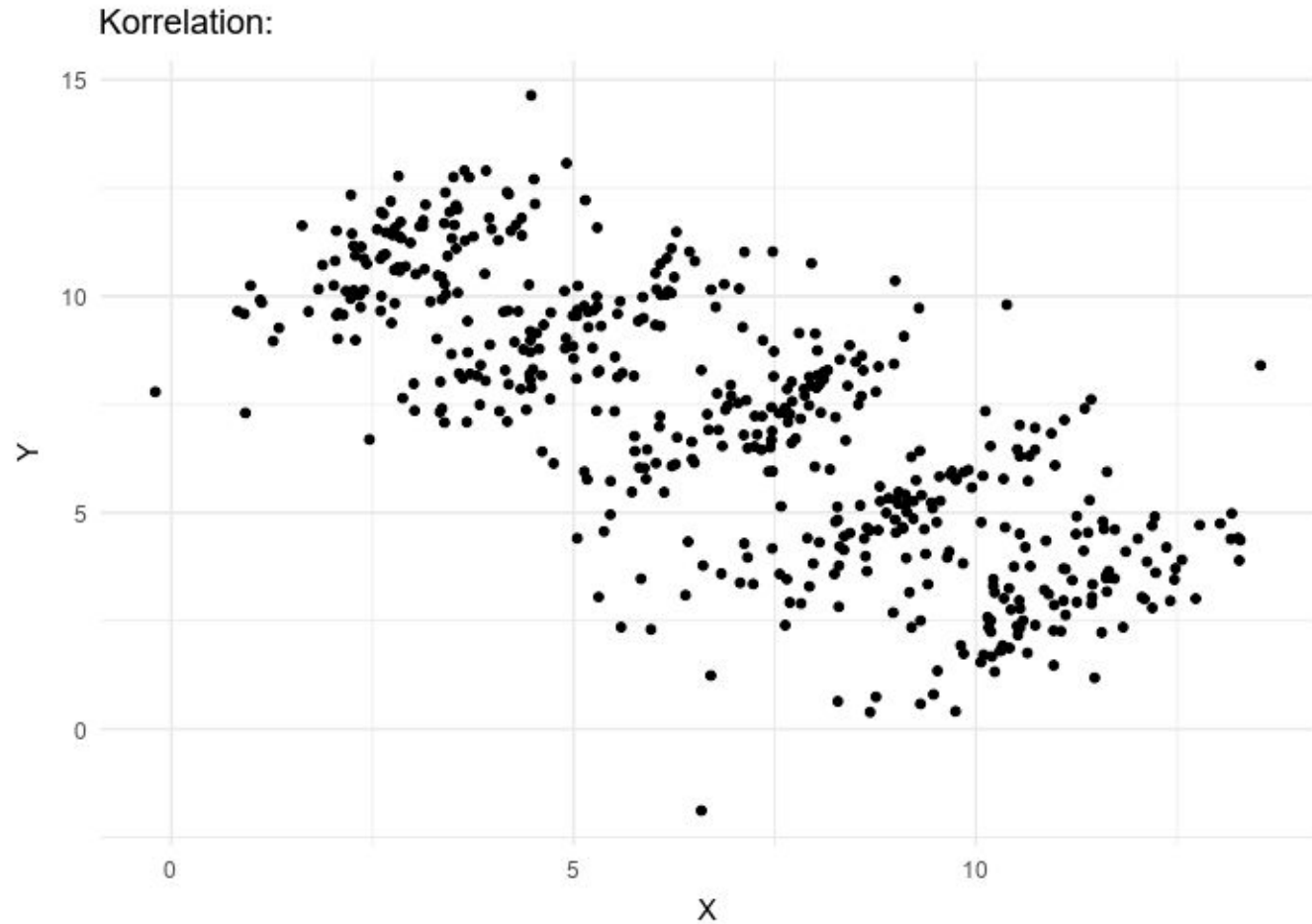


Quant + Quant: **Scatterplot**



Simpson's Paradox

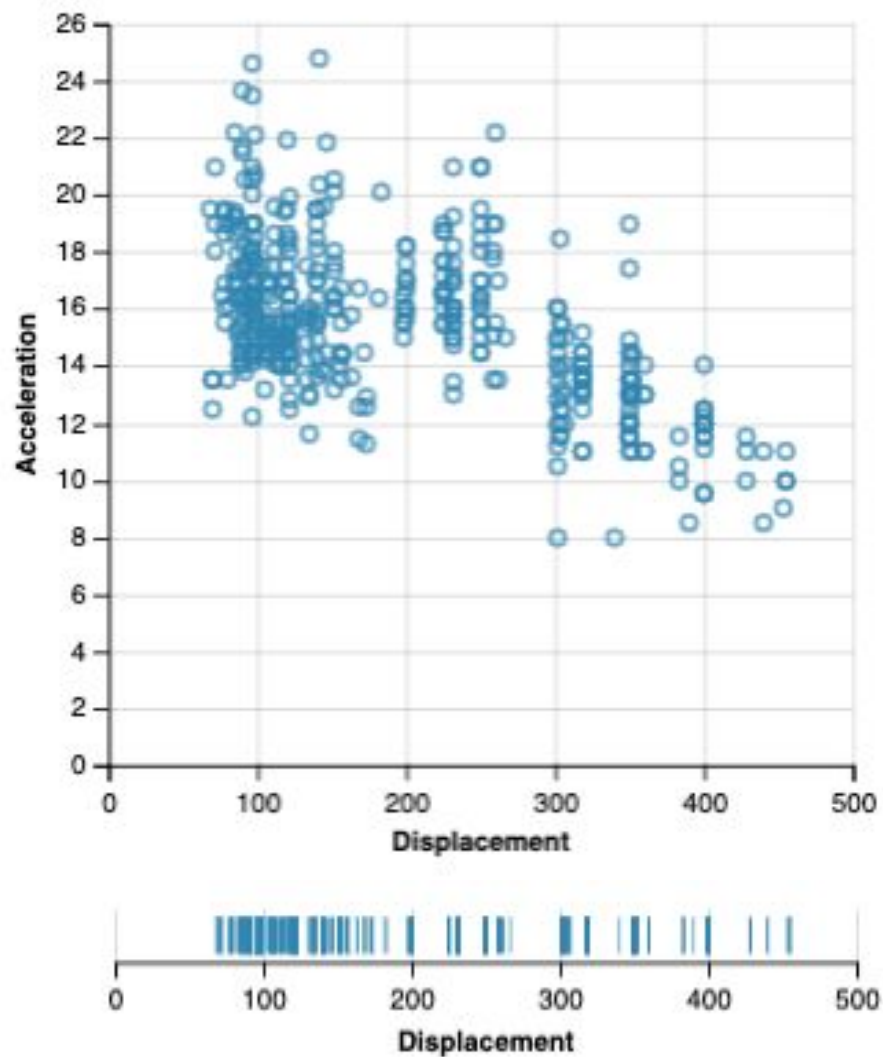
a trend appears in several different groups of data but disappears or reverses when these groups are combined.



Data types

	Quantitative	Ordered	Categorical
Quantitative			
Ordered			
Categorical			

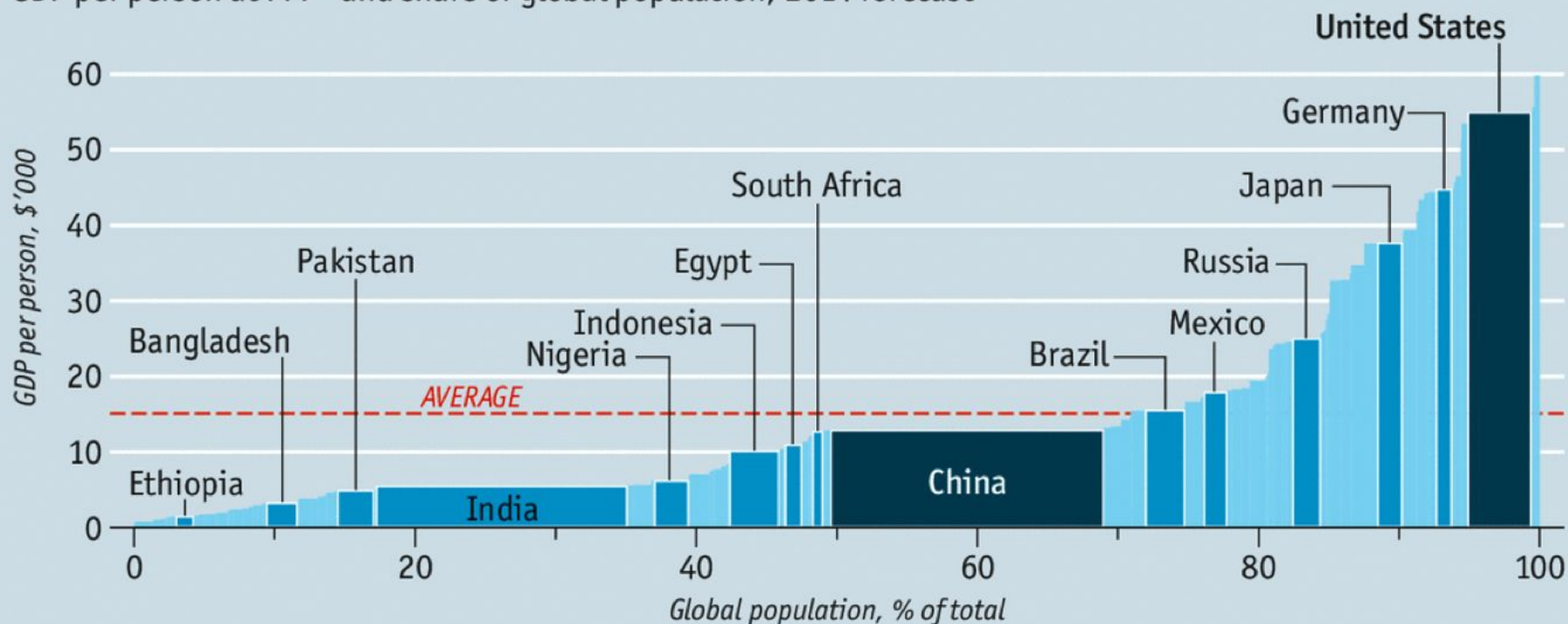
Quant x Quant: **Scatterplot**



Quant x Quant: **Mekko Chart**

A world of difference

GDP per person at PPP* and share of global population, 2014 forecast

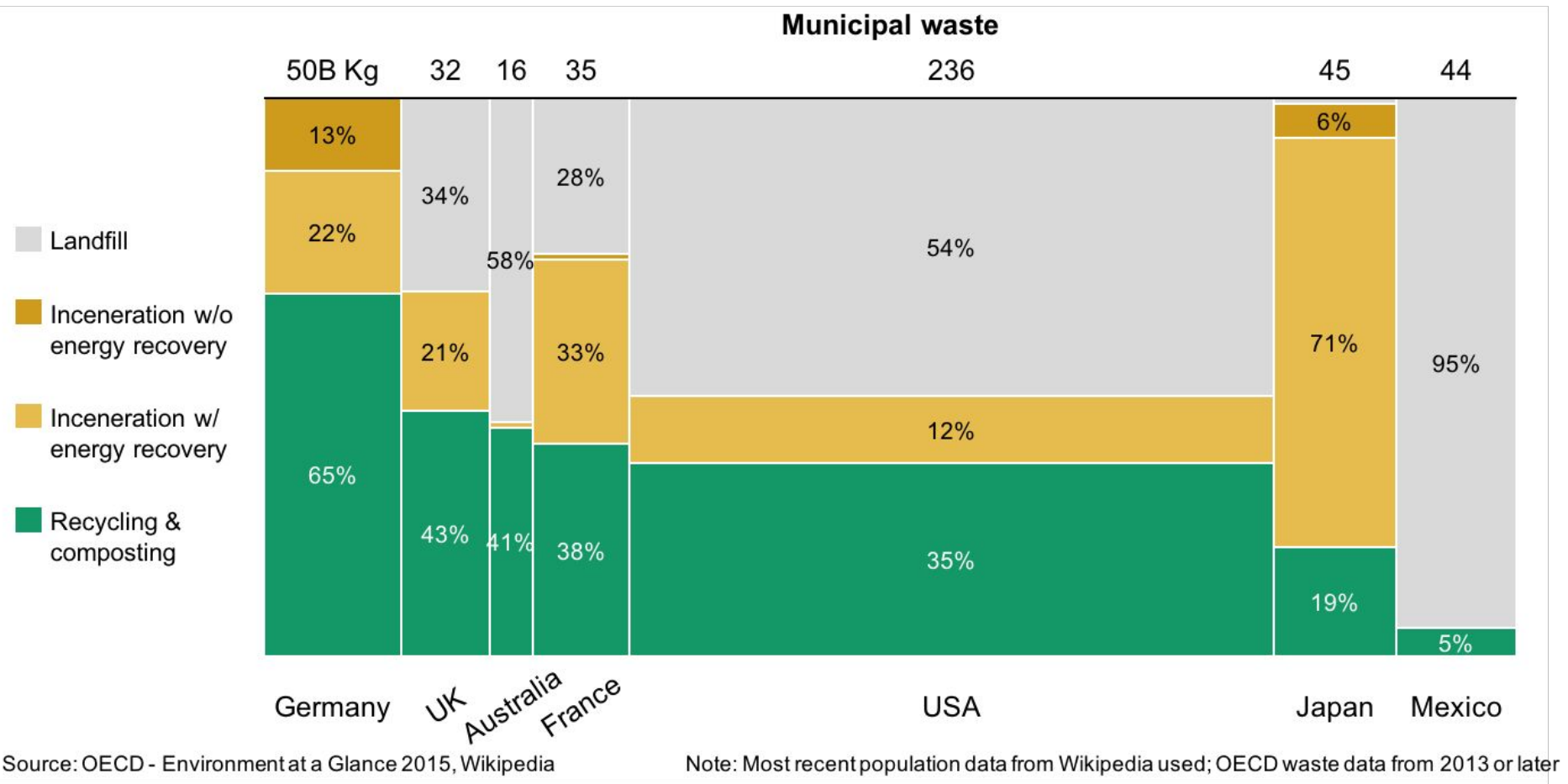


Sources: International Comparison Programme; IMF; *The Economist*

*Purchasing-power parity

Two quantities that if multiplied give a third quantity.

Quant x Quant: **Mekko Chart**

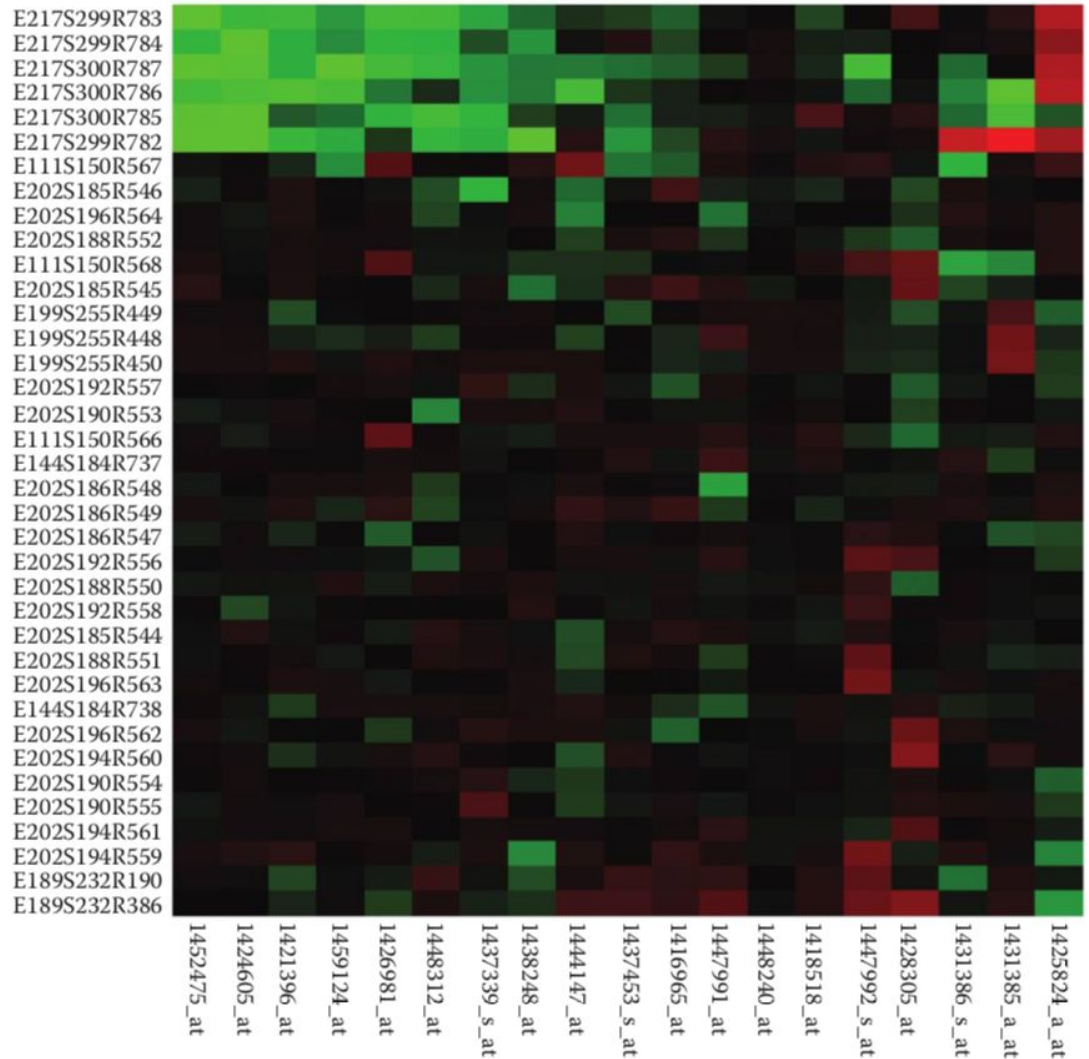


Two quantities that if multiplied give a third quantity.

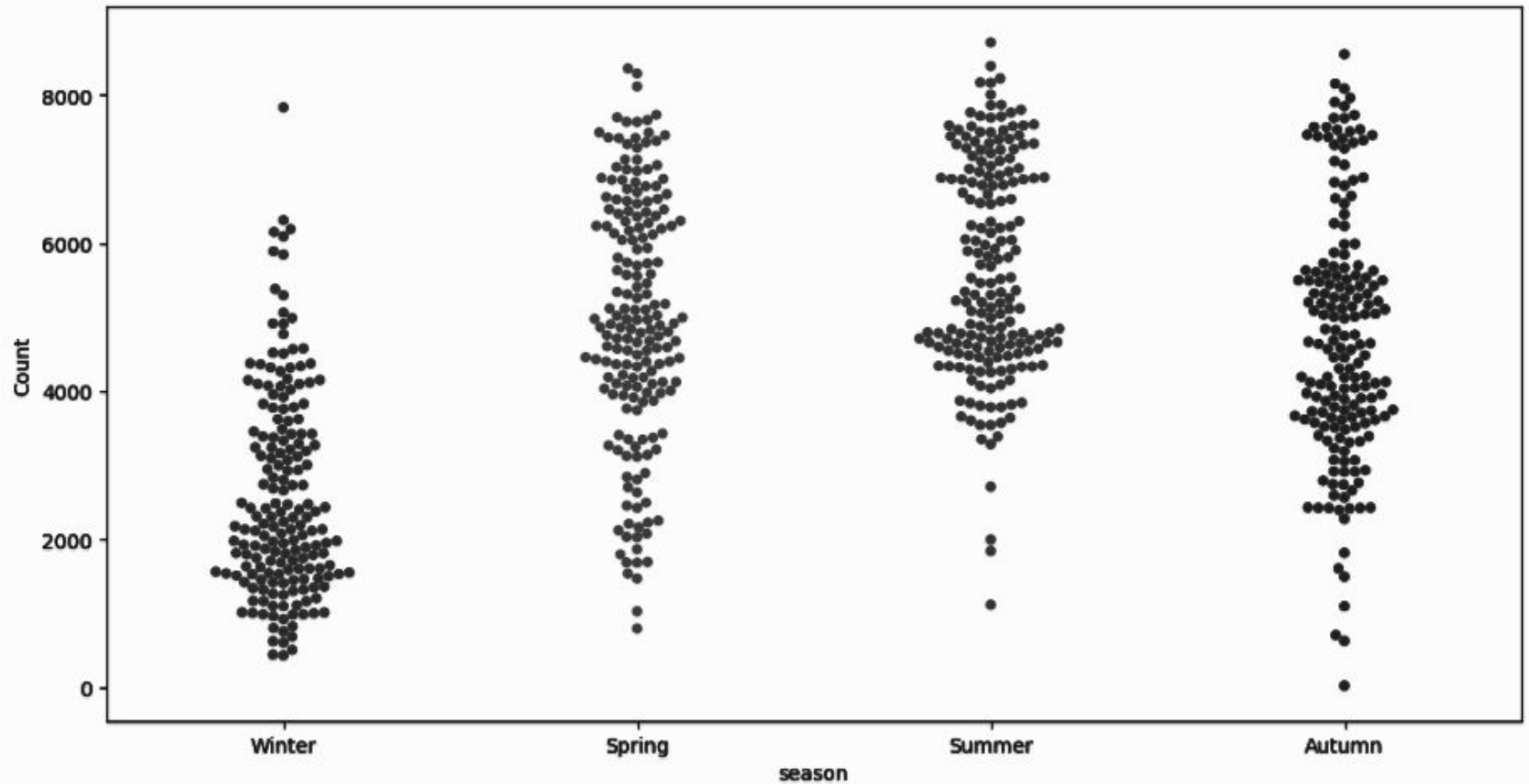
Quant + Ordered/Categorical: **Heatmaps**

A quantity (cells),
depending on two
factors (ordered or
categorical)

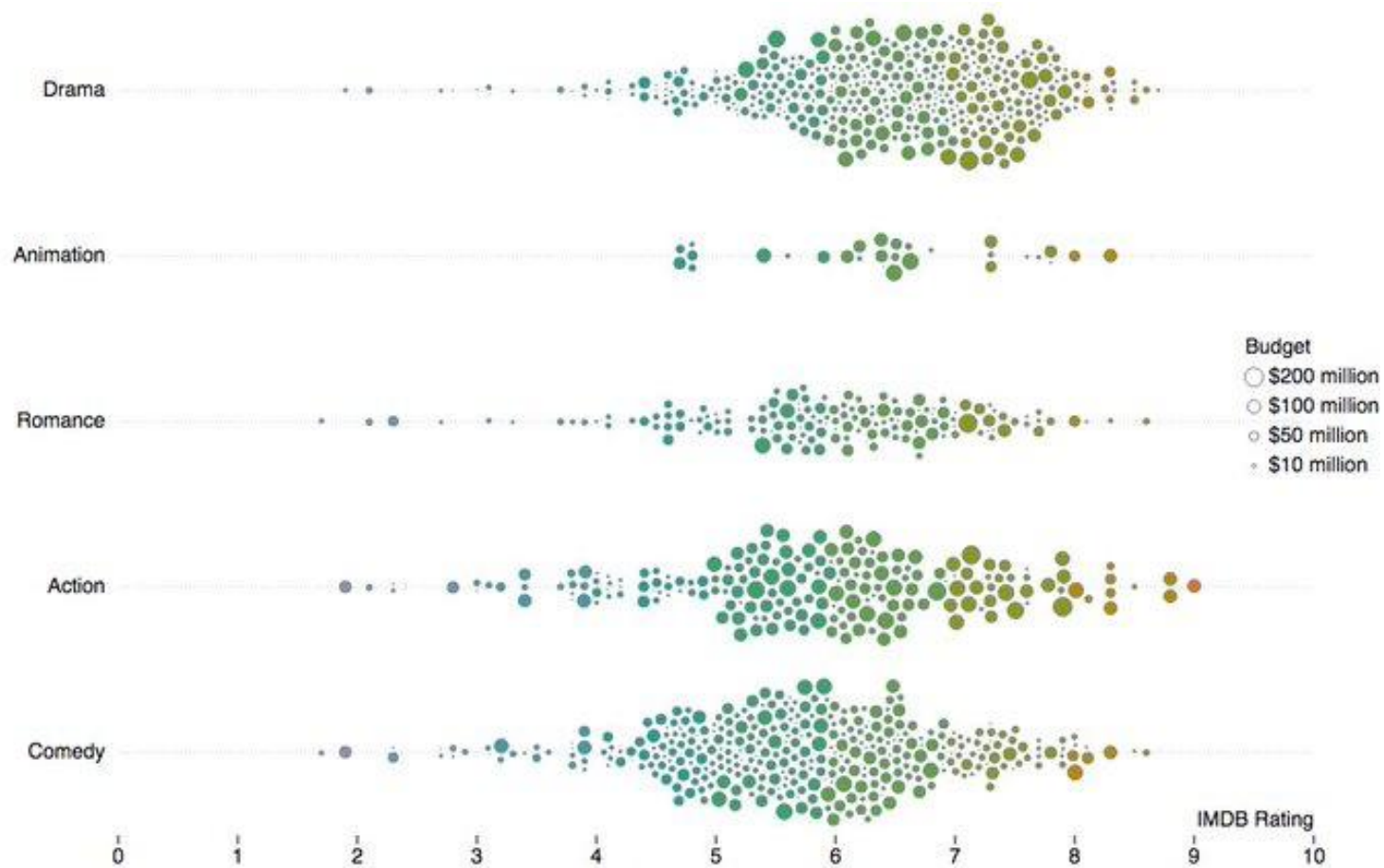
Requires complete
field.



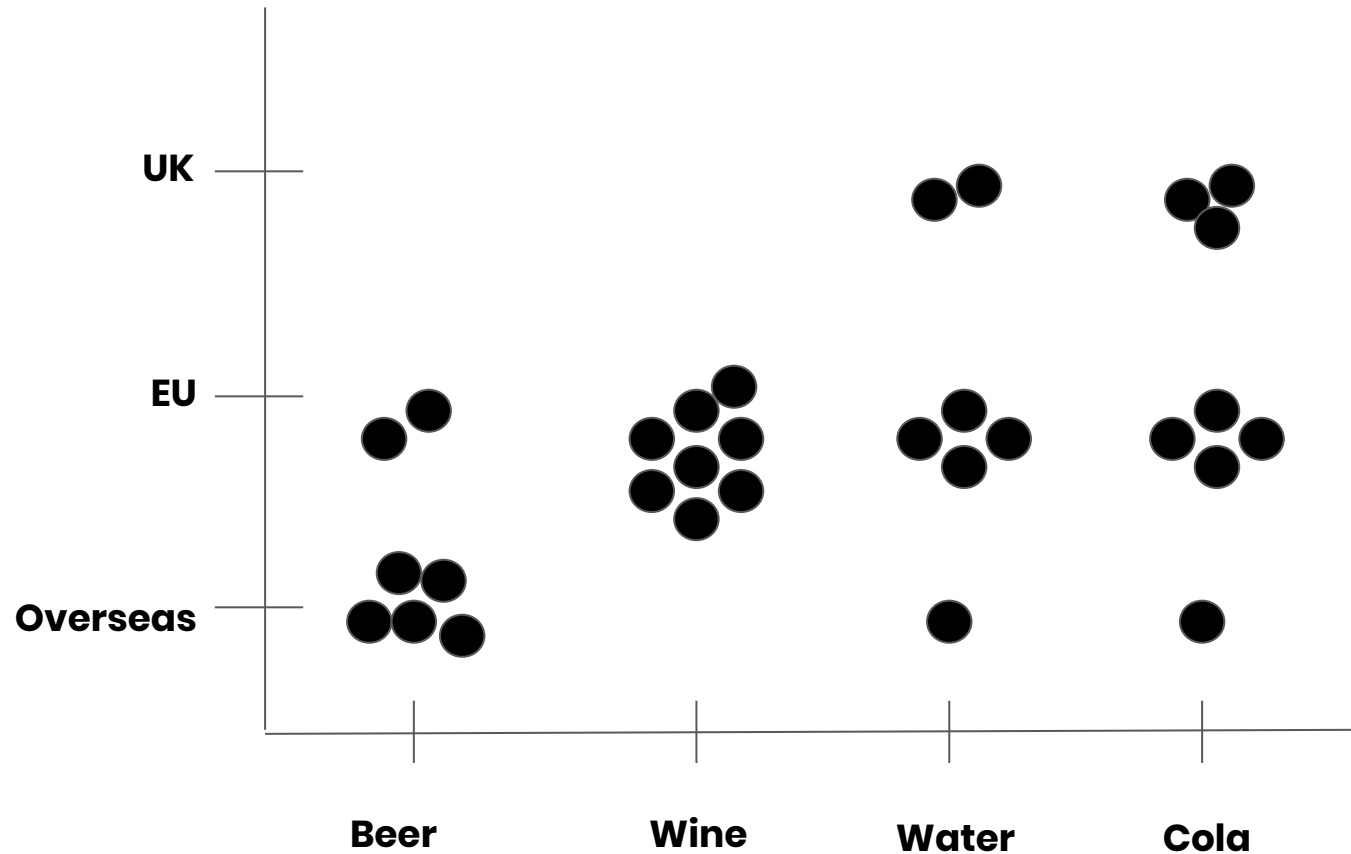
Quant + Ordered/Categorical: **Beeplots**



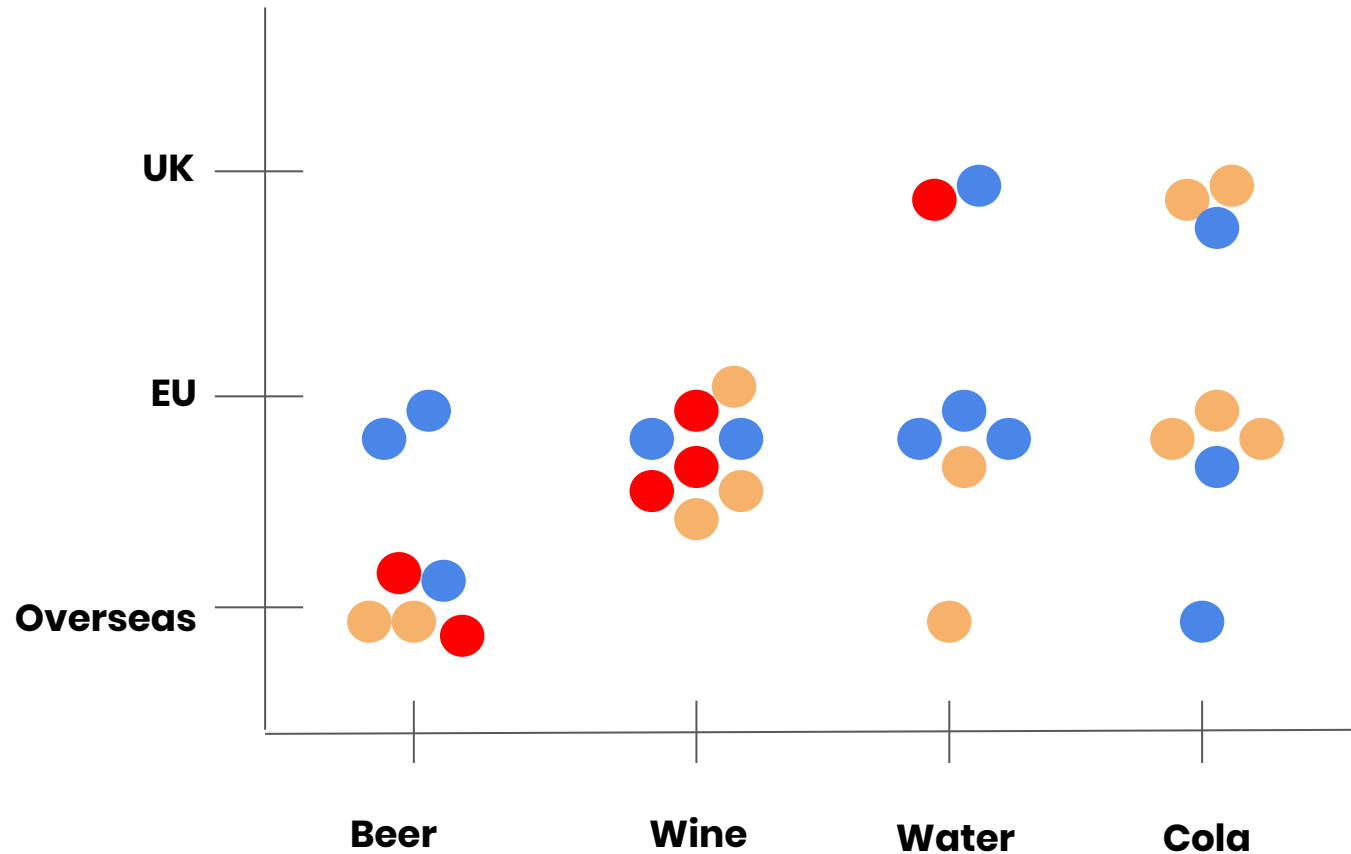
Quant + Categorical: **Swarm plots**



Categorical + Categorical: ***Swarm plots???***

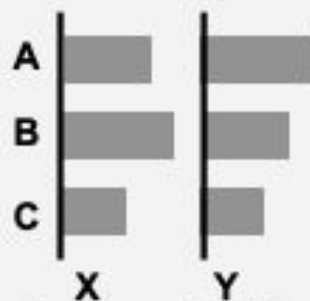


Categorical + Categorical: ***Swarm plots???***



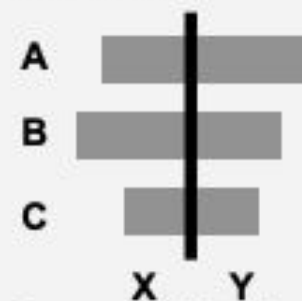
And again: **bar charts**

Bar Table X,Y



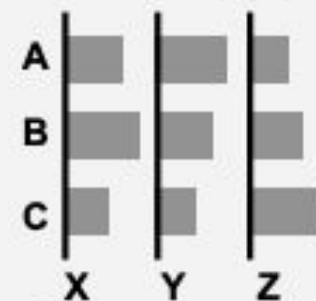
Compare X to Y,
'Small multiples'

Mirror Bar



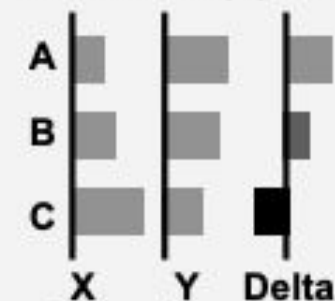
Compare X to Y

Bar Table X,Y,Z,...



Compare as many
as you like

Bar Table X,Y, Delta



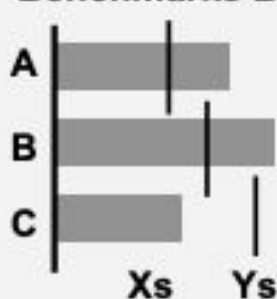
Comparisons are
slow. Plot critical
Deltas explicitly

Benchmark Bar



Compare X to a
benchmark

Benchmarks Bar



Compare X to Y.
Fancier version
called a 'Bullet graph'

Interleaved Bar



Compare X to Y
(not recommended)

Interleaves two
categories into
one spatial
dimension.
Typically better to
use Bar Table
(above) instead

... and many more!

Categories

Ordered Categories

Continuous Metrics

Metric, split by
1 category

Bar (Row)



Rows allow readable labels, while columns awkwardly turn text

Lollipop



More focus on the positions of tops. Fun factor +1

Dot Plot



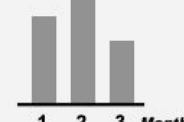
A non-zero y-axis base may be less misleading here

Bar (Column)



Histogram. Boxes help convey the underlying bins

Bar (Column)



Time moves horizontally. So use Column, not Row

Area



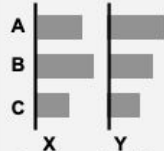
Adds continuity to x-axis

Line



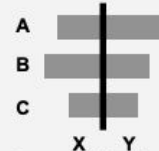
A non-zero y-axis base may be less misleading here

Bar Table X,Y



Compare X to Y, 'Small multiples'

Mirror Bar



Compare X to Y

Bar Table X,Y,Z,...



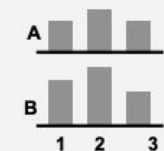
Compare as many as you like

Bar Table X,Y, Delta



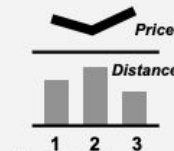
Comparisons are slow. Plot critical Deltas explicitly

Bar Table



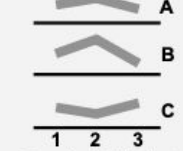
Compare a continuous metric across a category

Bar Line Table



Compare two metrics

Line Table



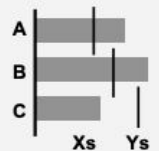
Trends visible, but use Lines (below) if precision is key

Benchmark Bar



Compare X to a benchmark

Benchmarks Bar



Compare X to Y. Fancier version called a 'Bullet graph'

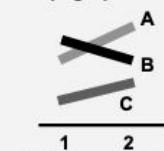
Interleaved Bar



Compare X to Y (not recommended) ←

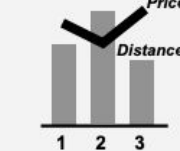
Interleaves two categories into one spatial dimension. Typically better to use Bar Table (above) instead

Slopegraph



With two values, slope encodes delta

Dual Axis



Use (above) instead. Crossings here are salient, but meaningless

Lines



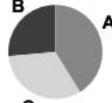
Compare many. Getting spaghetti? Use Line-Table (above)

... by
2+ categories

... and much more!!!

... by Part-to-Whole, split by 1 category
2+ categories

Pie



Screams 'Percentages!'

Stacked Bar (Row)



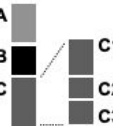
More precise and flex, but less screaming

Stacked Bar (Col)



Now I'm standing

Breakout Bar



Let's zoom in here. User different colors. Global starts left (or top)

Waterfall



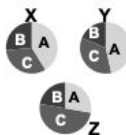
Waterfalls are vertical stacked bars that narrate financial values in a (typically) artificially imposed ordering

These lines are identical, with equal vertical separation at each X



Beware of an illusion for these: seeing differences (lines), or category values (stacked area) can be difficult and even misleading

MultiPie



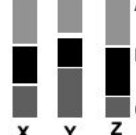
Please don't... (not recommended)

Stacked Bars (R)



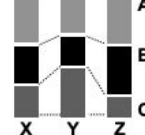
...Use this instead

Stacked Bars (C)



Horizontal flow implies an ordering

... with lines

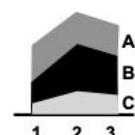


Added lines suggest continuity, help depict changes

No legends. Instead, directly label actual values



Stacked area



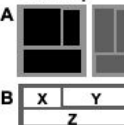
Now it's definitely continuous

Mekko stacks in X and Y simultaneously. Here XYZ might be absolute values of a market, and ABC are company market shares as %s

Mekko



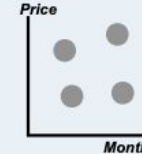
Treemap



Hierarchy, ~3 levels max. Size & color code different metrics. Often misused (info)

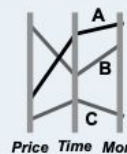
Metrics: relationships to other metrics

Scatter



A most powerful chart

Parallel Coordinates



Price Time Month Instead of Perpendicular Cartesian axes, Parallel format allows more axes

Look at this number Just look at it.



Dot Array



Dot Array %

43% Huge Number

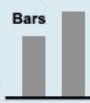


Icon Array (ISOTYPE, info)



Icon Array %

Connecting Lines imply continuous data



USA Dutch

Same data, ask people, "What do you see?"

"Dutch people are taller than Americans"

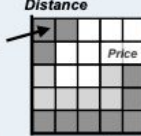


USA Dutch

"People get taller as they get more Dutch"

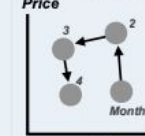
Zacks & Tversky, 1997

2D Heat



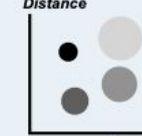
2D Histogram

Connected Scatter



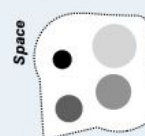
The power of a scatterplot, with points connected by time (info)

Rosling Scatter



Watch Hans Rosling's famous TED talk. He adds two more metrics, and moves it over time

Map

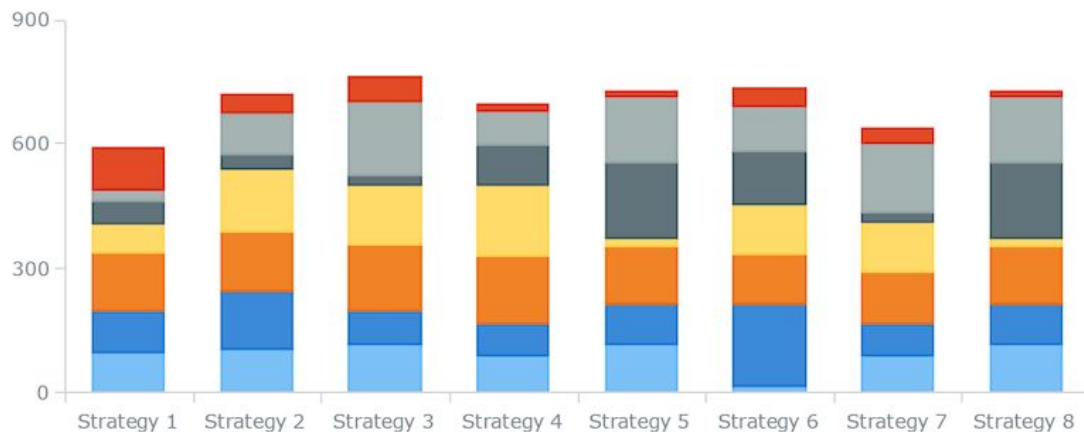


Maps and scatterplots share the same DNA Color = Flight Time Size = Price

Stacked Bar Charts



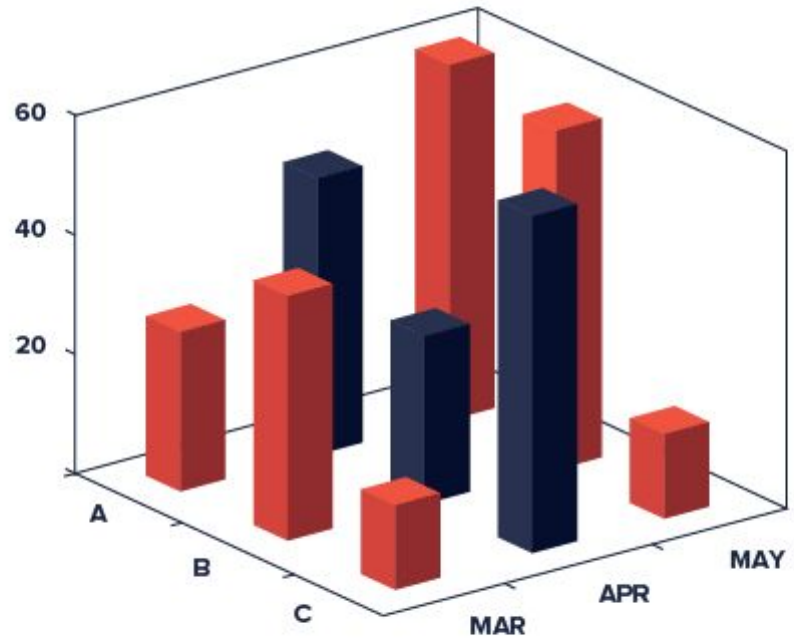
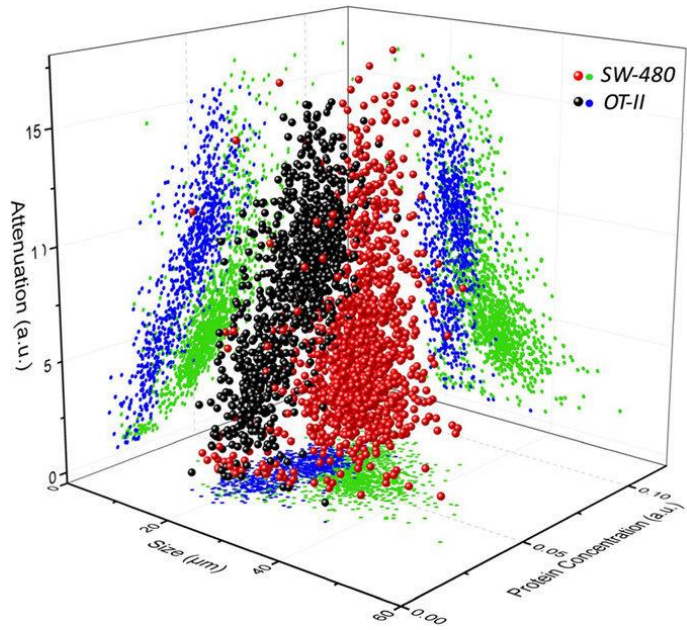
- Individual distributions
- Individual value comparison
- Details



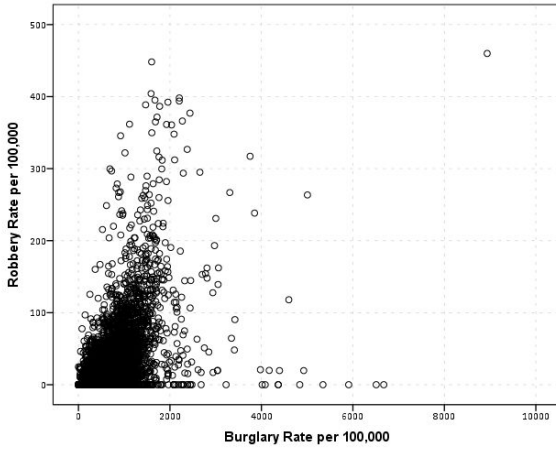
- Sum comparison
- Overview

> requires good color palette!

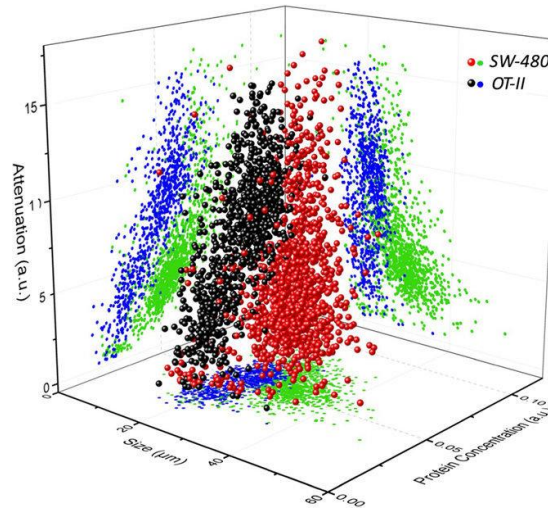
3 Dimensions...



...4 Dimensions?



2-dimensional

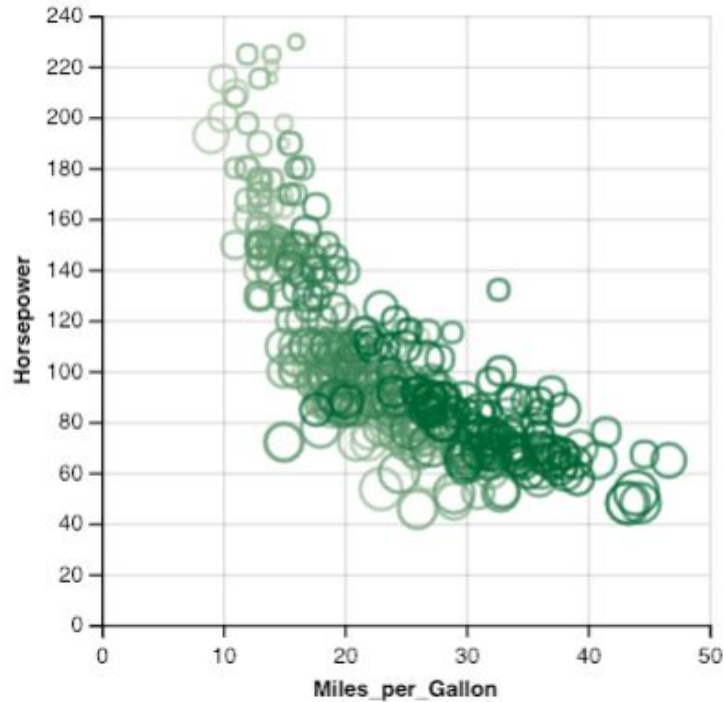


3-dimensional

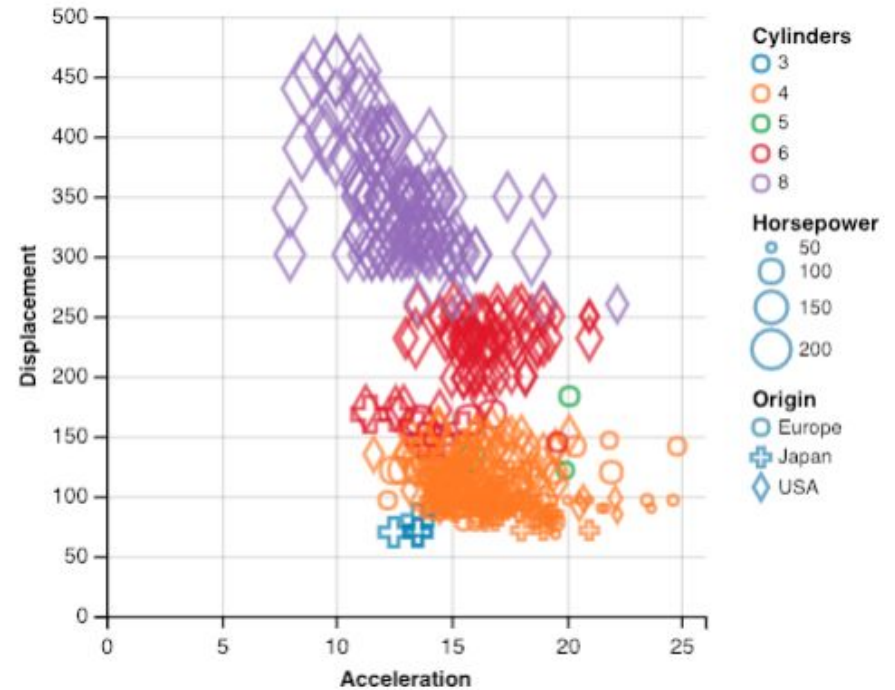
?

3-dimensional

1. Additional Visual Variable(s)

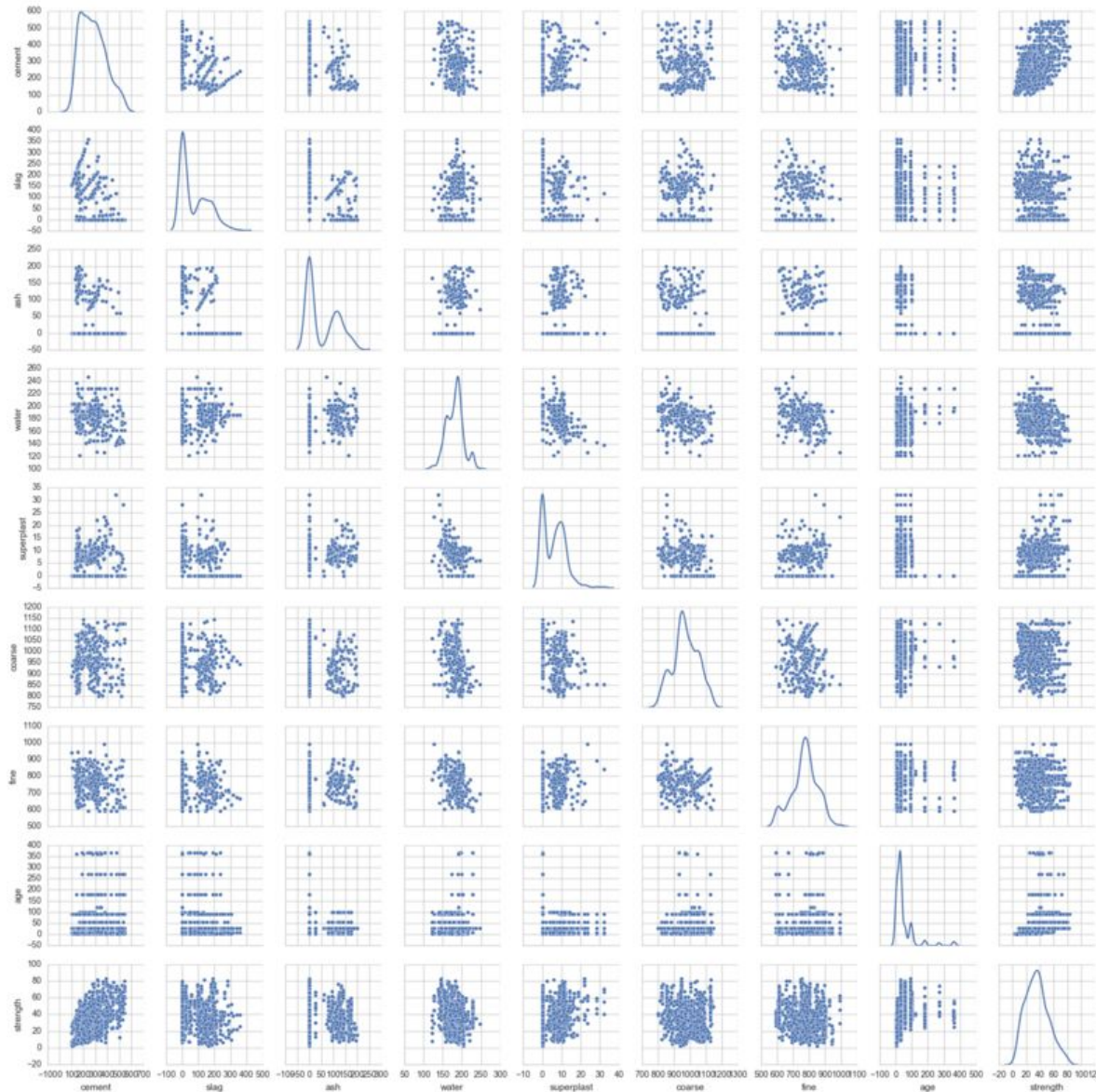


2-dimensional
+ 1 dimension (size)



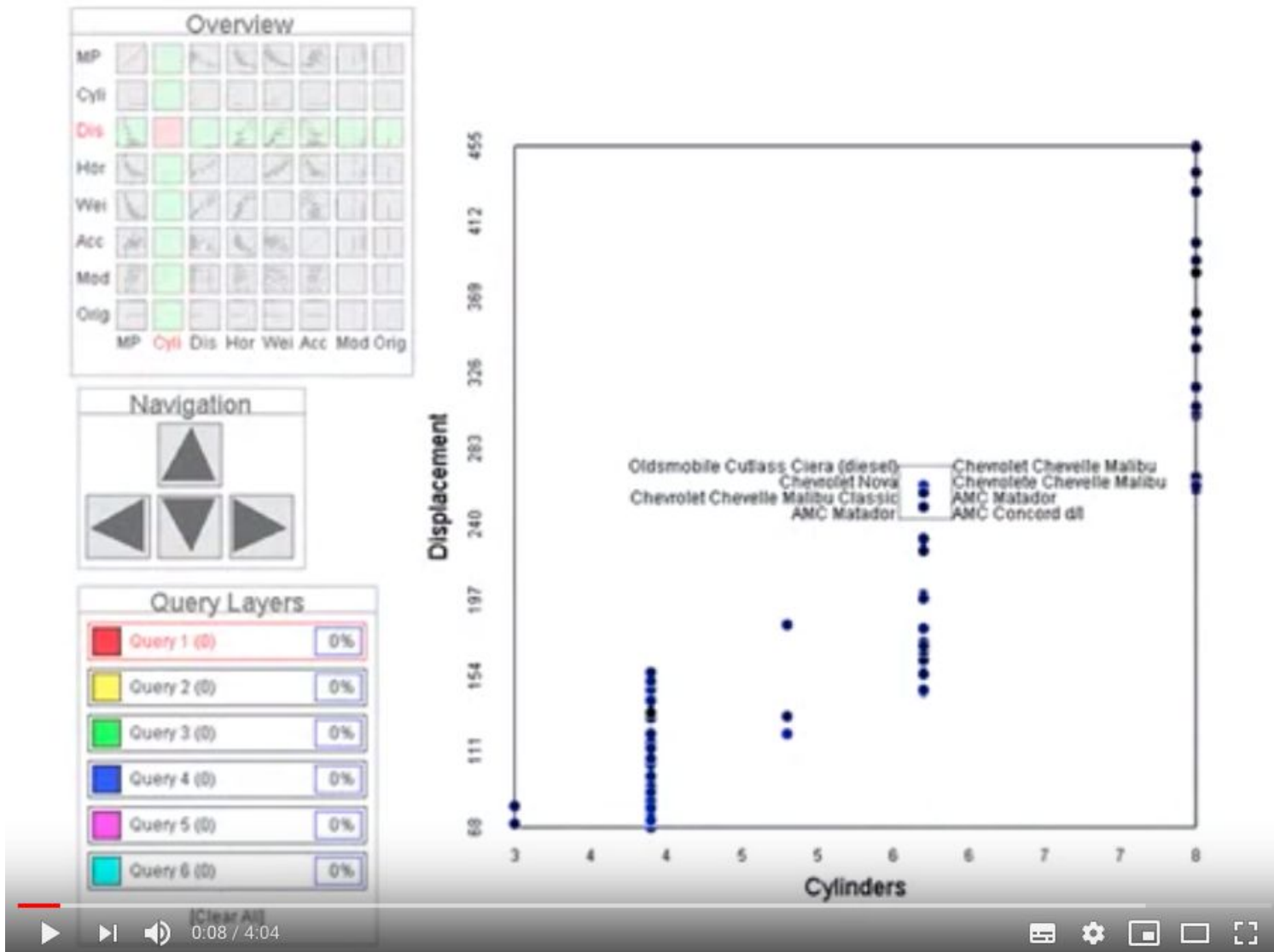
2-dimensional
+ 2 dimension
(shape + color)

2. Pairwise comparison: **Scatterplot Matrix**



- + Scalable
 - + Provides overview
 - + Can use additional visualizations
 - + Easy to understand and decode
-
- Many dimensions require pan+zoom

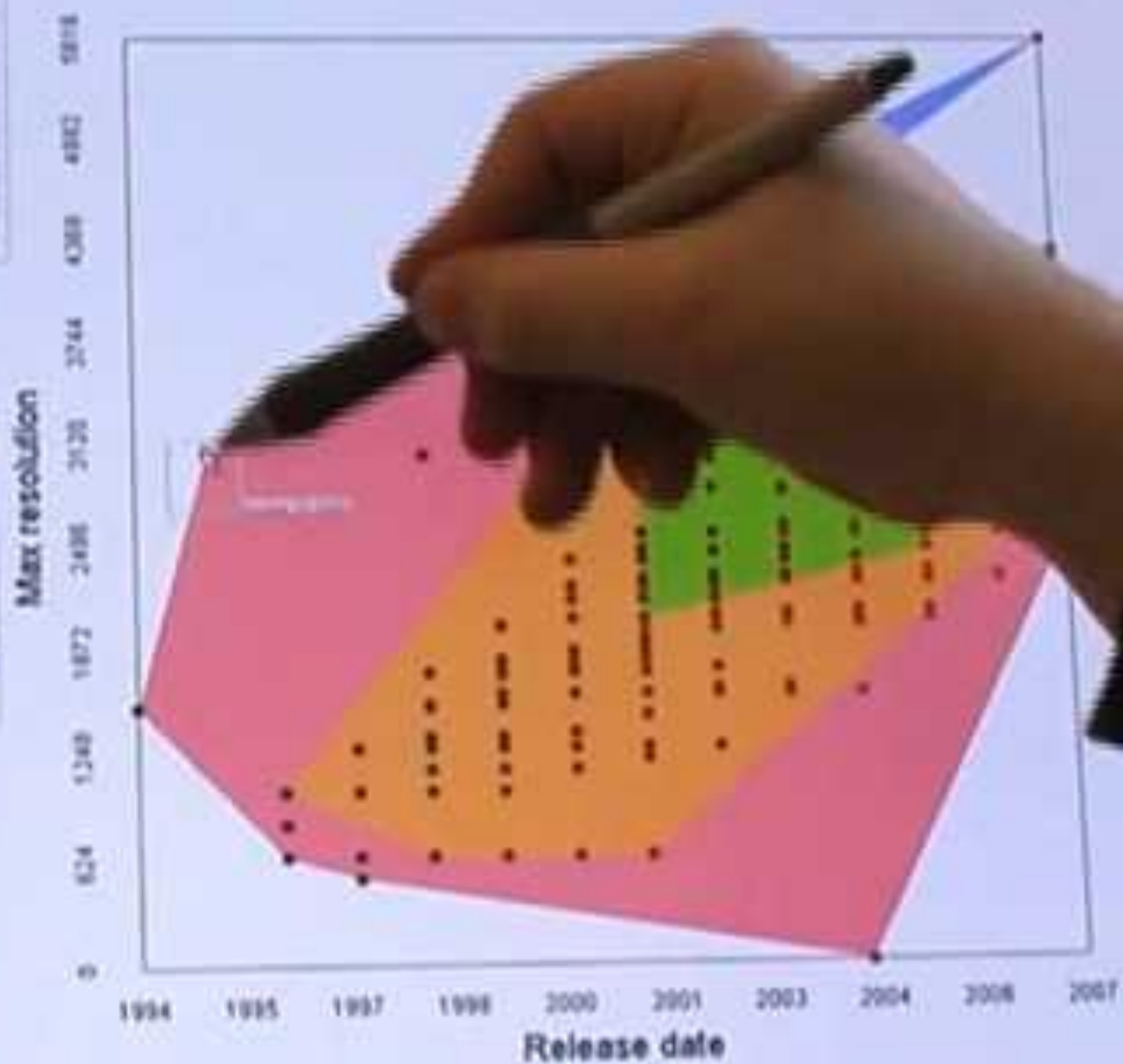
Scatterplot Navigation: Scatterdice



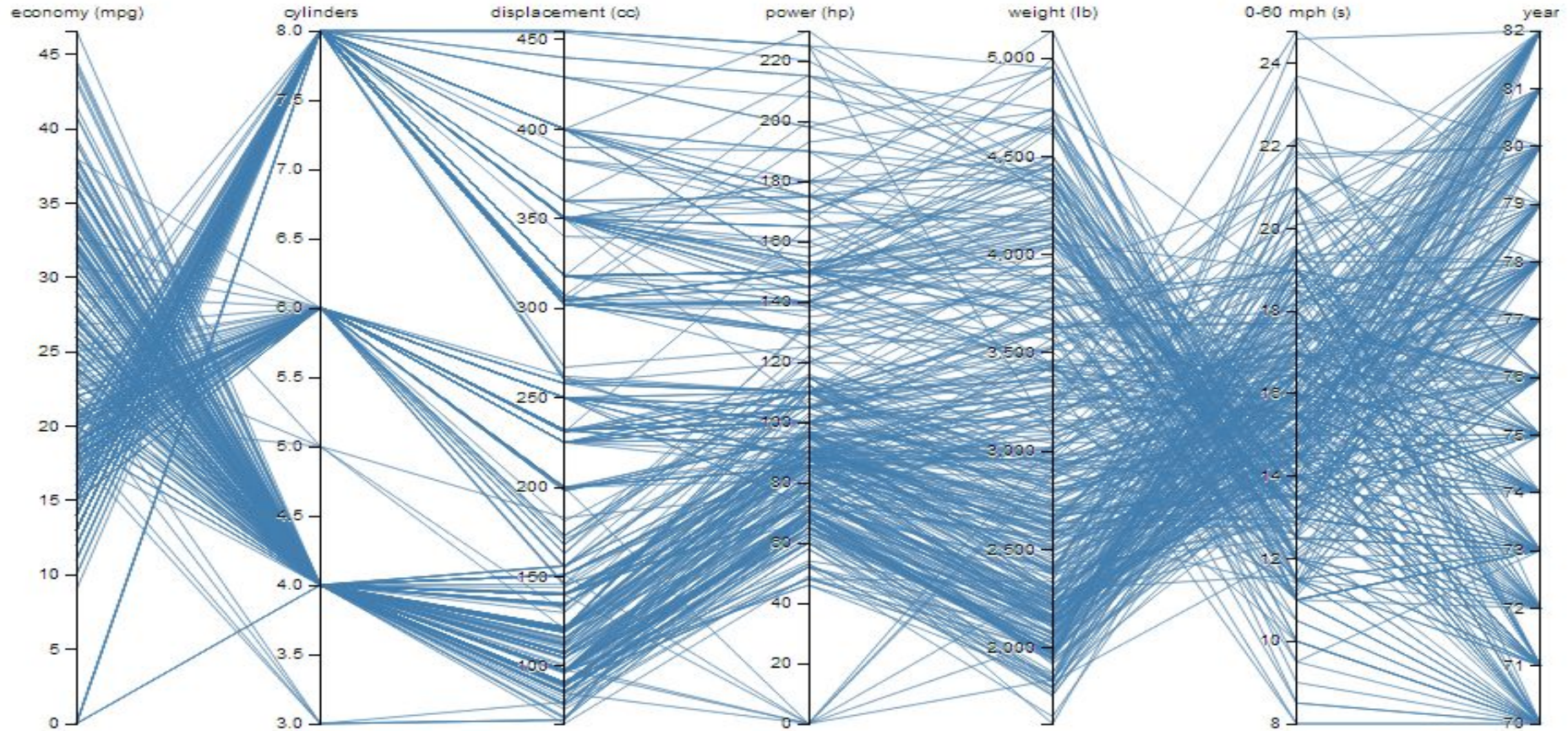
Elmqvist, Niklas, Pierre Dragicevic, and Jean-Daniel Fekete. "Rolling the dice: Multidimensional visual exploration using scatterplot matrix navigation." *IEEE transactions on Visualization and Computer Graphics* 14.6 (2008): 1539-1148.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100

Query Layers		
Query 1 (2000)		1.0
Query 2 (2000)		1.0
Query 3 (2000)		1.0
Query 4 (2000)		1.0
Query 5 (2000)		1.0
Query 6 (2000)		1.0
© 2000		

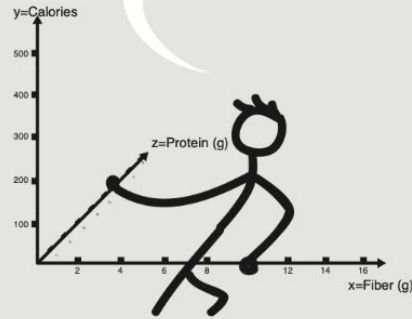
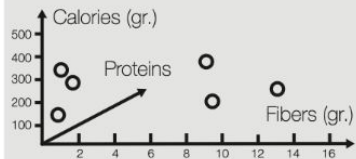


4. Parallel Coordinates Plot (PCP)

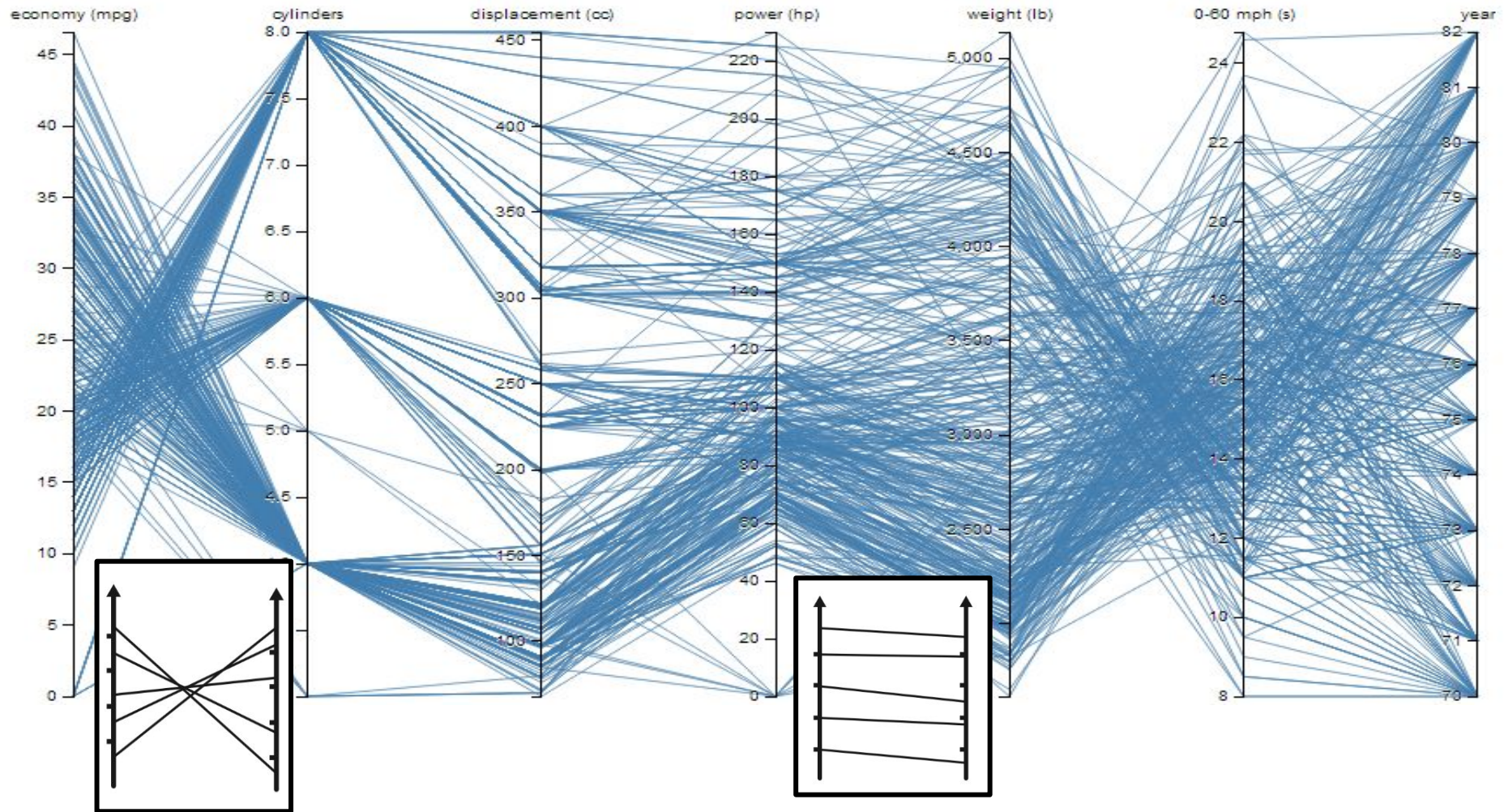


4. Parallel Coordinates Plot (PCP)

Let's change the arrangement of the axes...



4. Parallel Coordinates Plot (PCP)

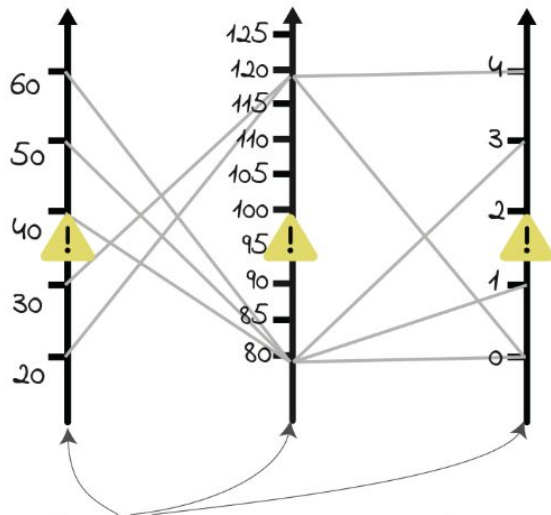


- + Scalable
- + Consise
- + Good overview

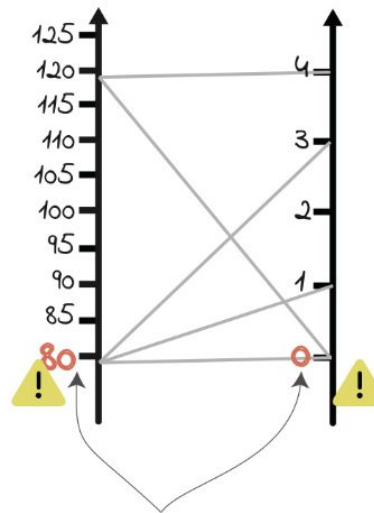
- Depending on ordering
- Can suffer from clutter
- Visual path following can be hard

PCPs Pitfalls

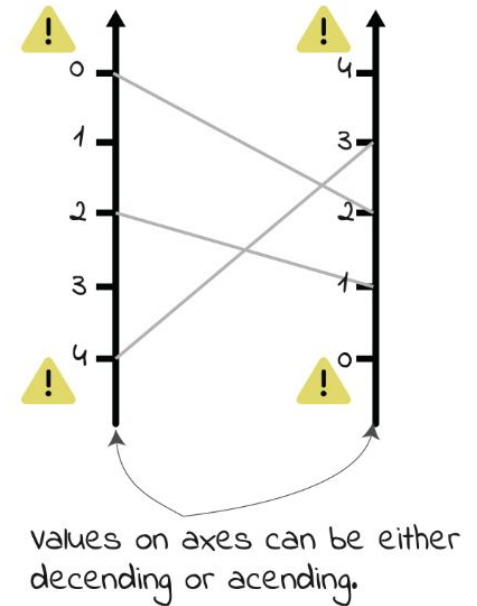
Axis scales



Truncated axes



Axes order



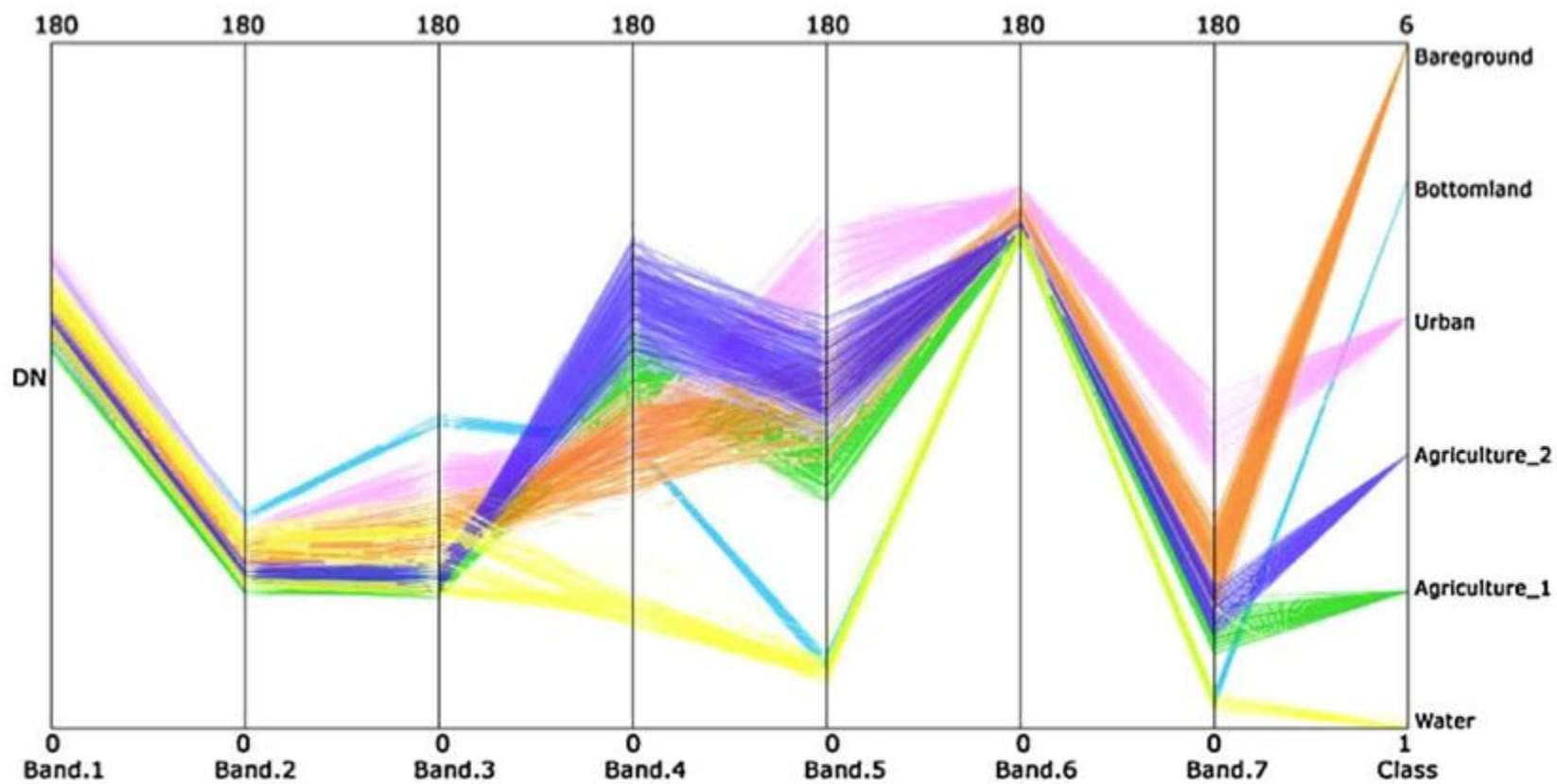
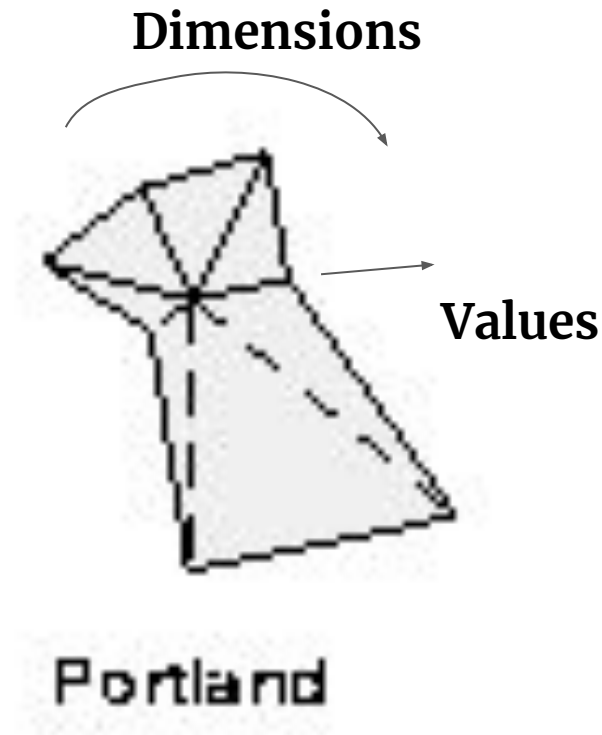


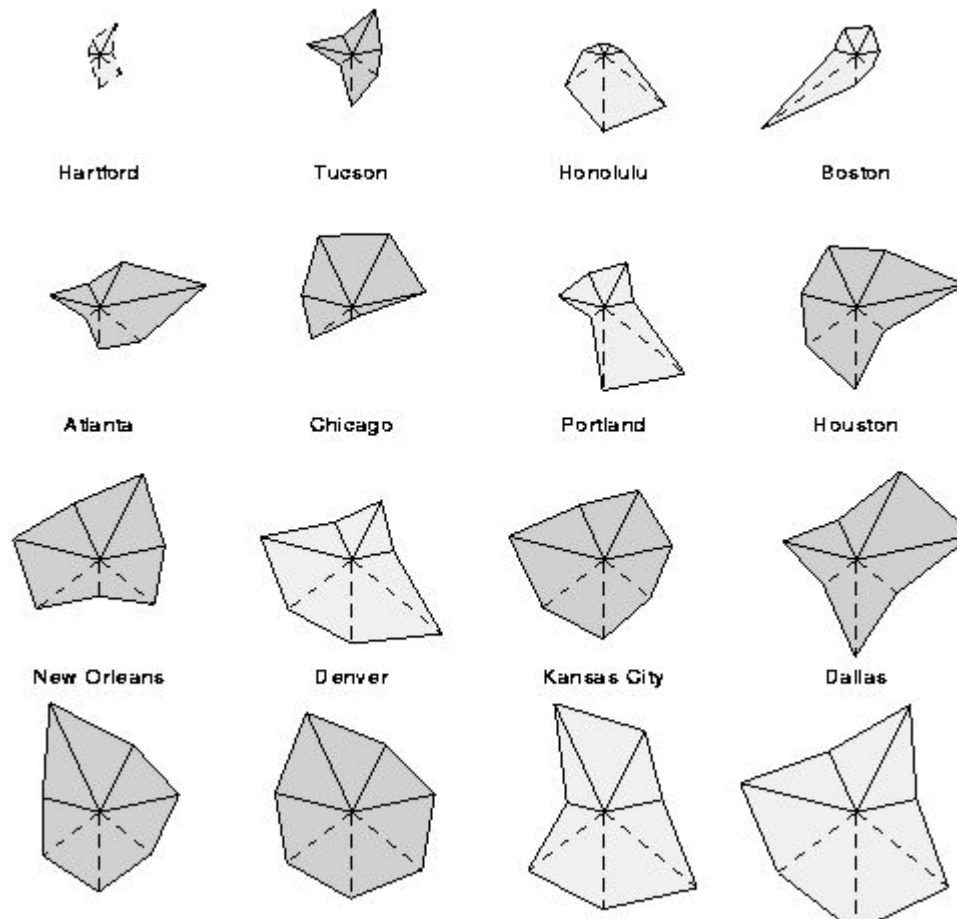
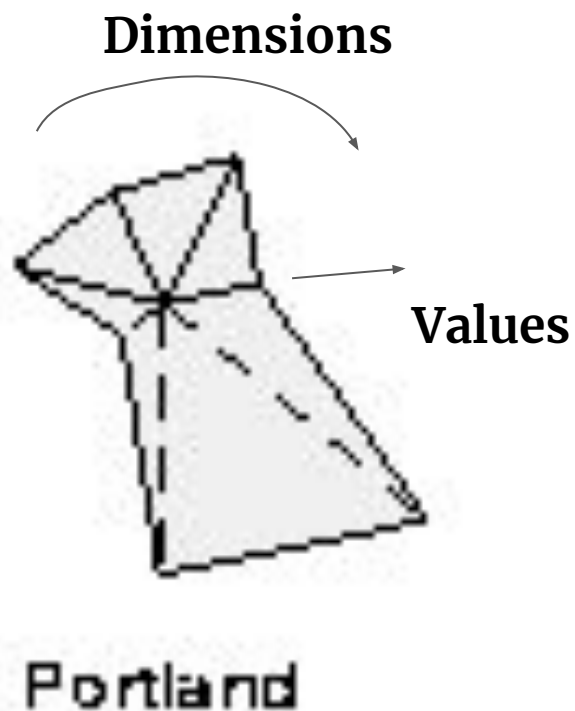
Fig. 3. PCP of sample data.

3. Glyphs: Star glyphs



- 1) Data glyphs are [a] technique, in which single data points are encoded individually by assigning their dimensions to one or more marks and their visual variables
- 2) Each glyph can be placed spatially independently from others

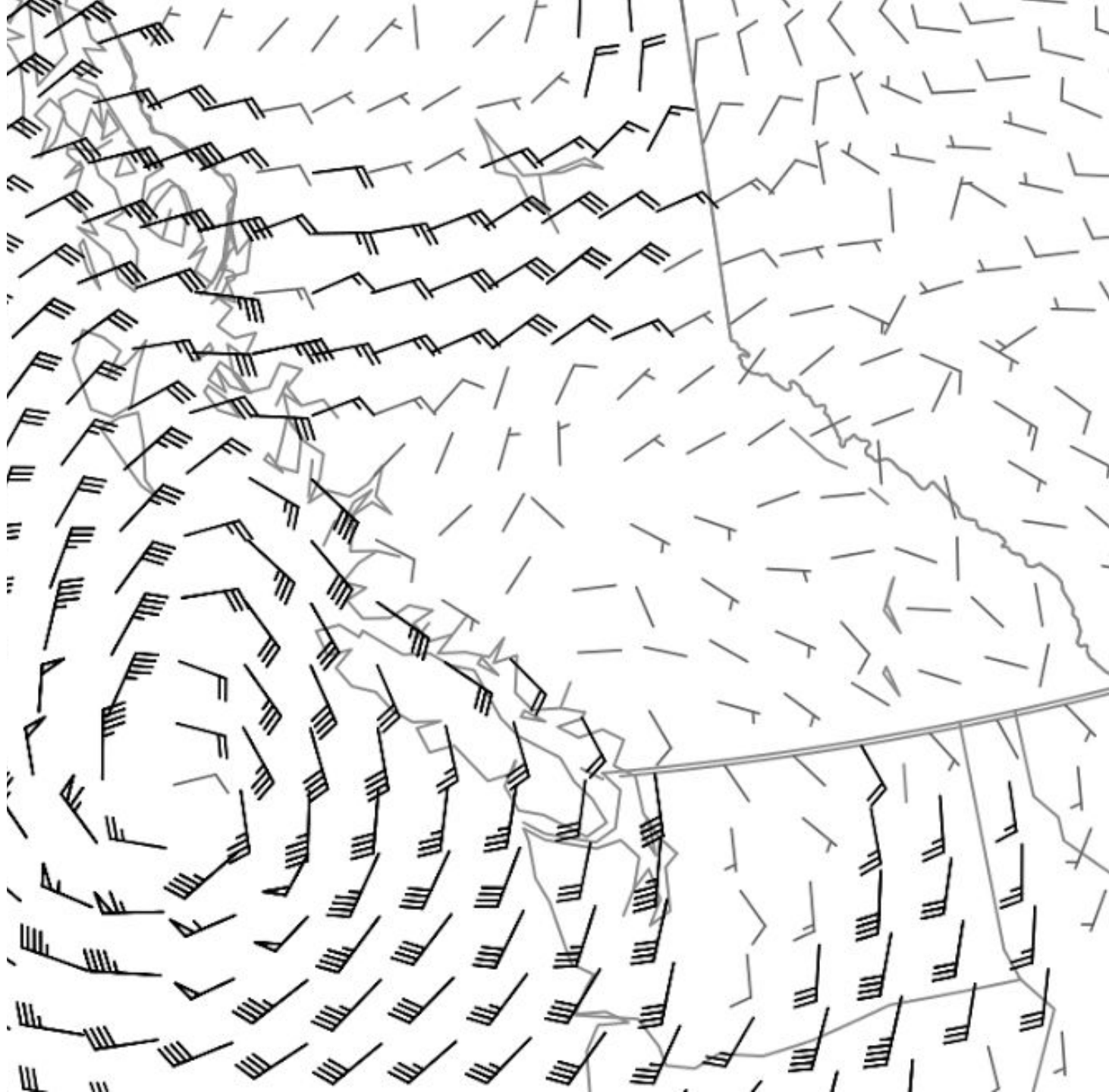
3. Glyphs: Star glyphs



- + Comparison
- + Outlier, Trends
- + Individual values

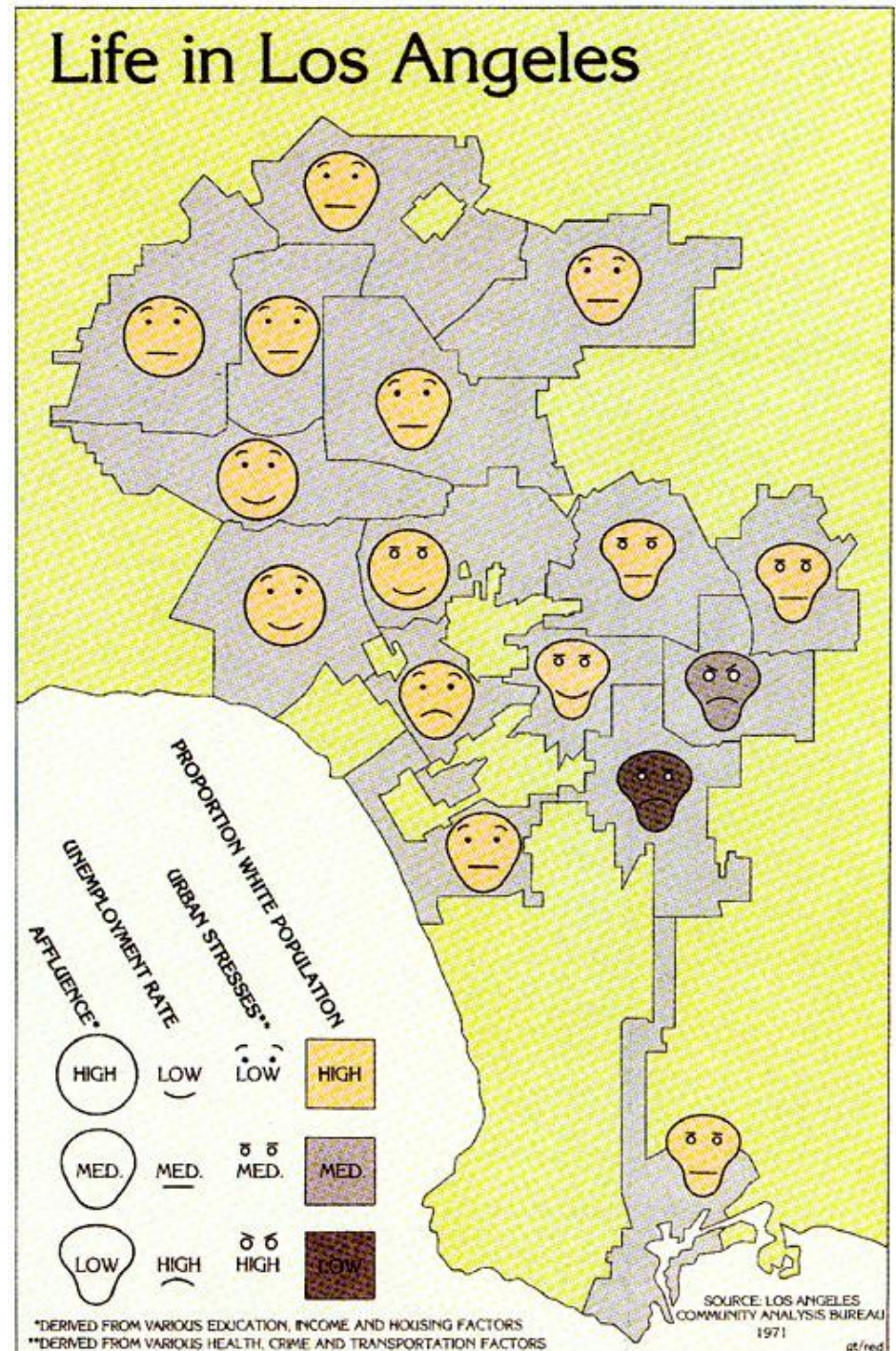
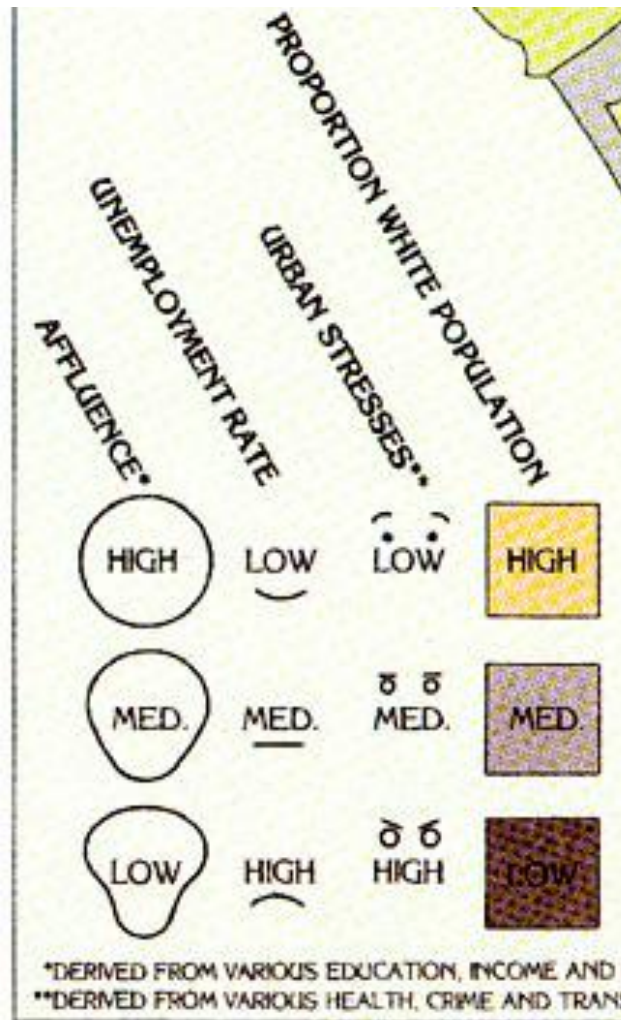
- Precise comparison
- Cluster dimensions

Weather glyphs



Chernoff Faces

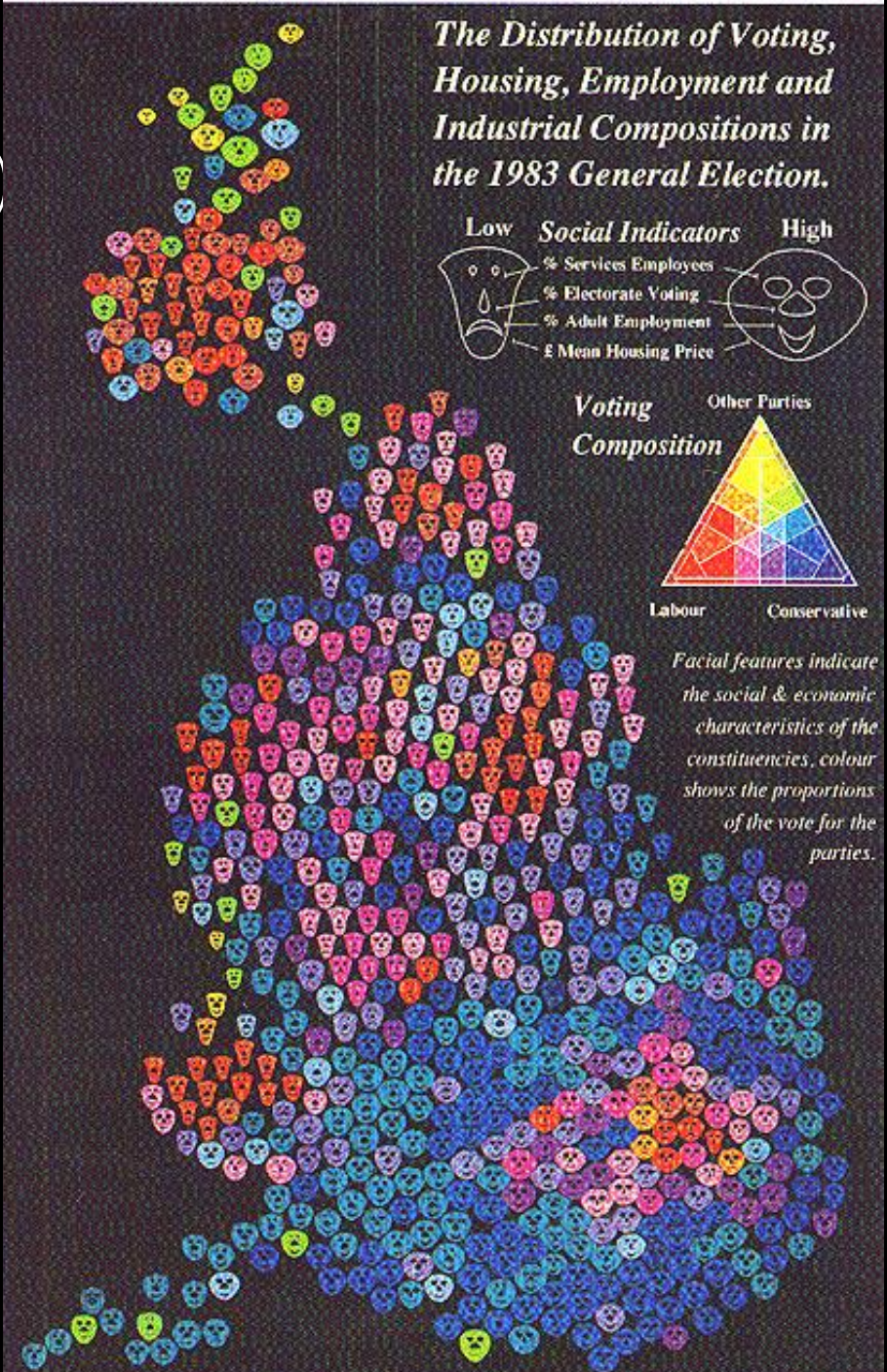
(Glyphs for geodata)



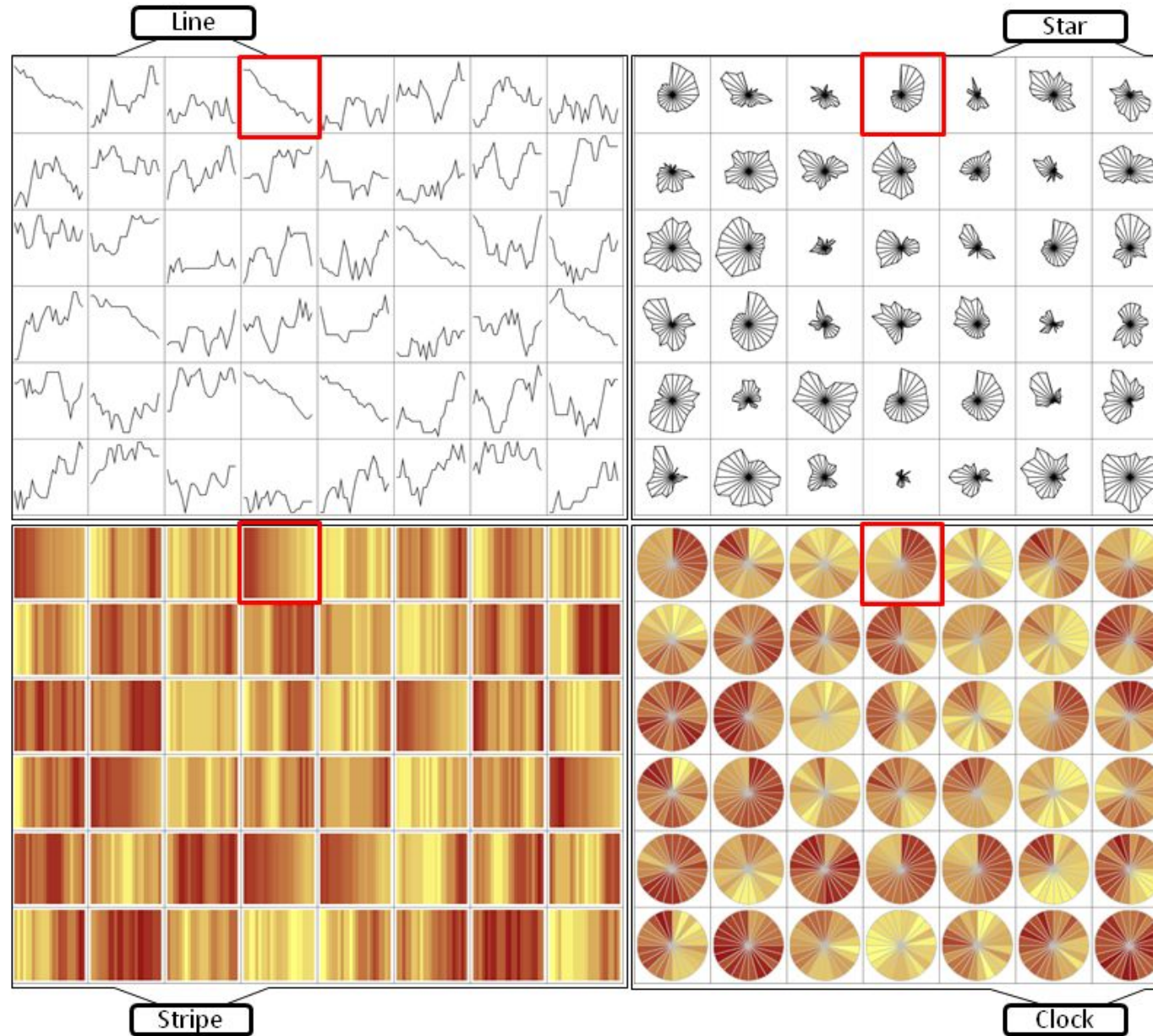
Chernoff Faces

(Glyphs for geodata)

- + Individual values
- + Spatial correlation
- Some vis-variables are more prominent
- Some vis-variables are hard to perceive and estimate

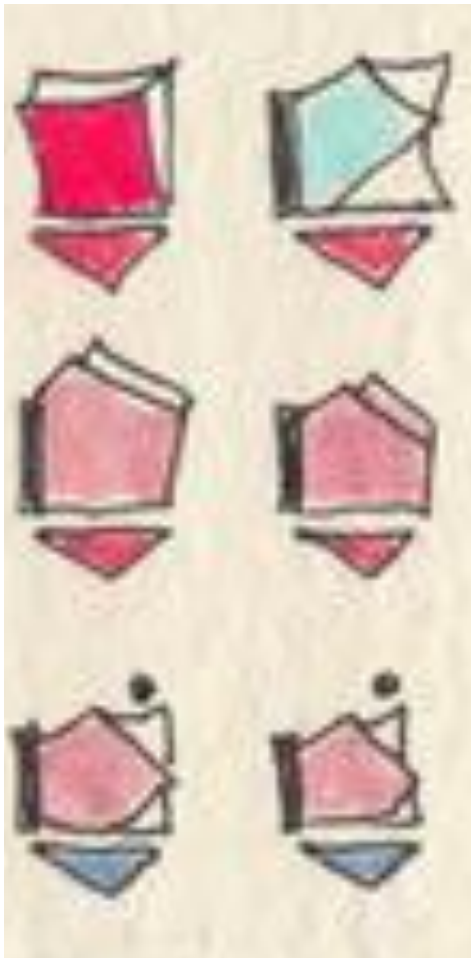


Glyphs for Temporal data



- Lineglyphs for trends and peaks
- Radial for value look-up

Dear Data (fantastic glyphs)



66 Dear Data

WEEK 52 - ... Goodbye! **Last week of Dear Data*

HOW TO READ IT:



This week I tracked all the "Goodbyes / ByeByes / goodnight" I said. Each Element is a goodbye I said, in chronological order.

SHAPE = "HOW"

□ = in real life

◻ = over the phone

◻ = skype / hangout

◻ = in public (public speech)

◻ = farewell to my old apartment!

* = missed goodnight to my boyfriend 'cause I fell asleep too early

physical contact:

color = to whom?

color of the triangle = did I add something?

◻ = good luck!

◻ = have fun / enjoy / divert!

◻ = talk soon / see you later / a dopo!

◻ = thanks! / thanks for... / grazie

◻ = Bacchus!

◻ = have a nice day / evening

◻ = love you!

* kiss
• hug
o hand-shake
(no physical contact if dot is missing)

- mum
- boyfriend
- friend
- you and Rebecca
- coworker
- acquaintance
- client
- grandma
- stranger (sales man / waitress...)

from: G. LUP

Brooklyn NY - USA



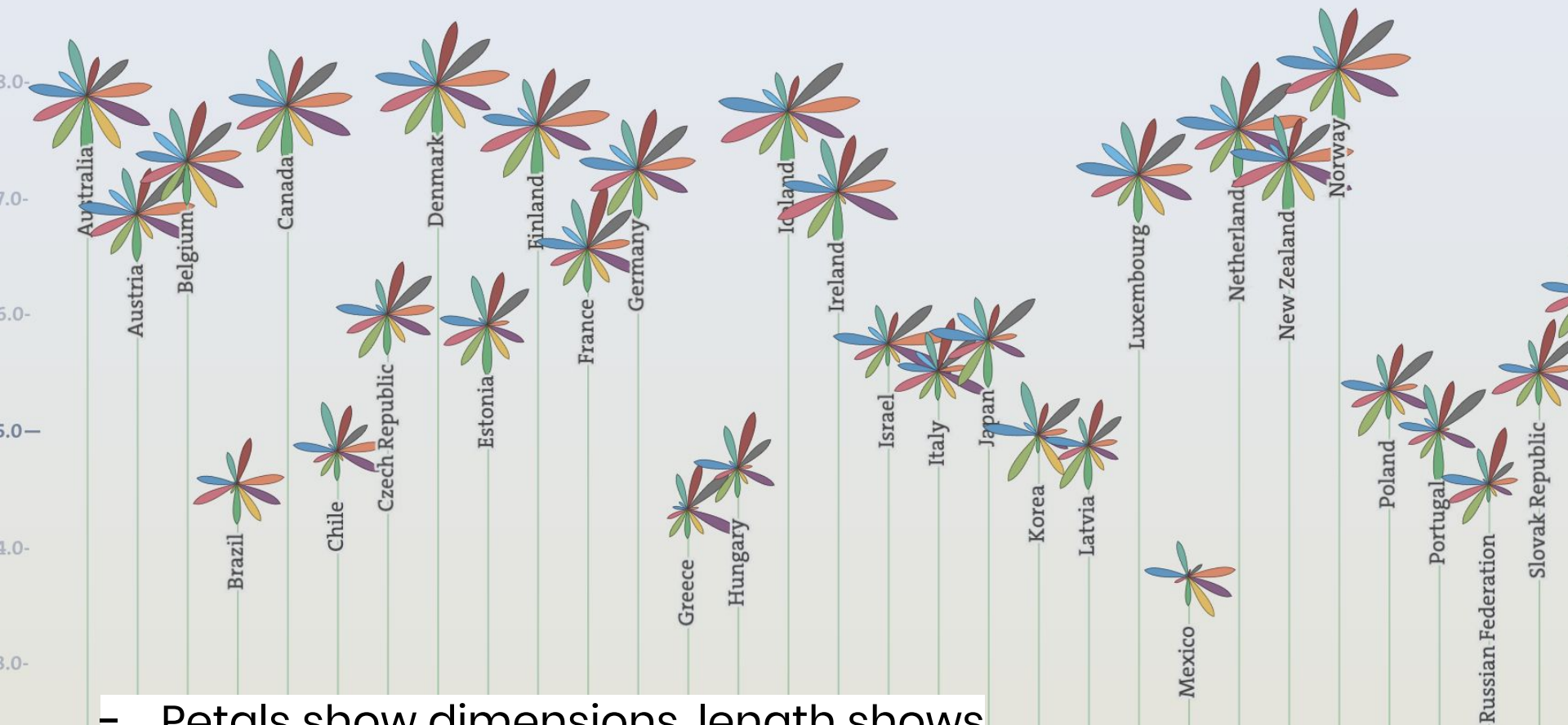
SEND TO:

STEFANIE POSAVEC

LONDON

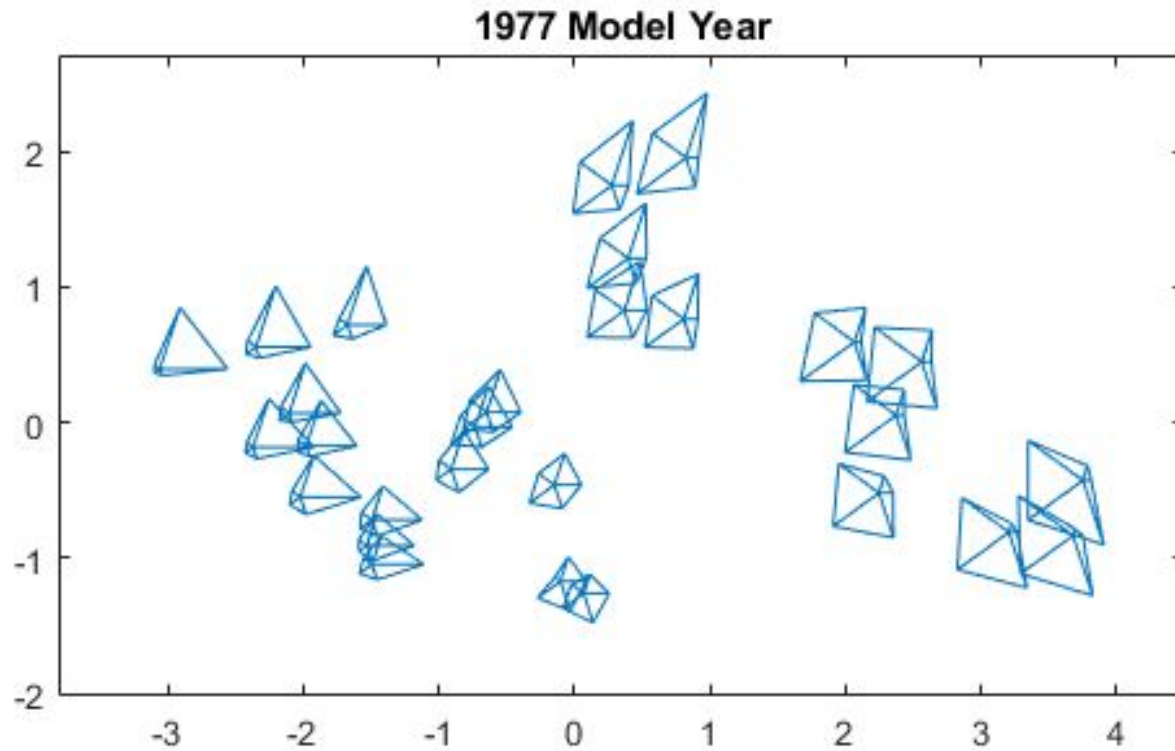
- UK -

England

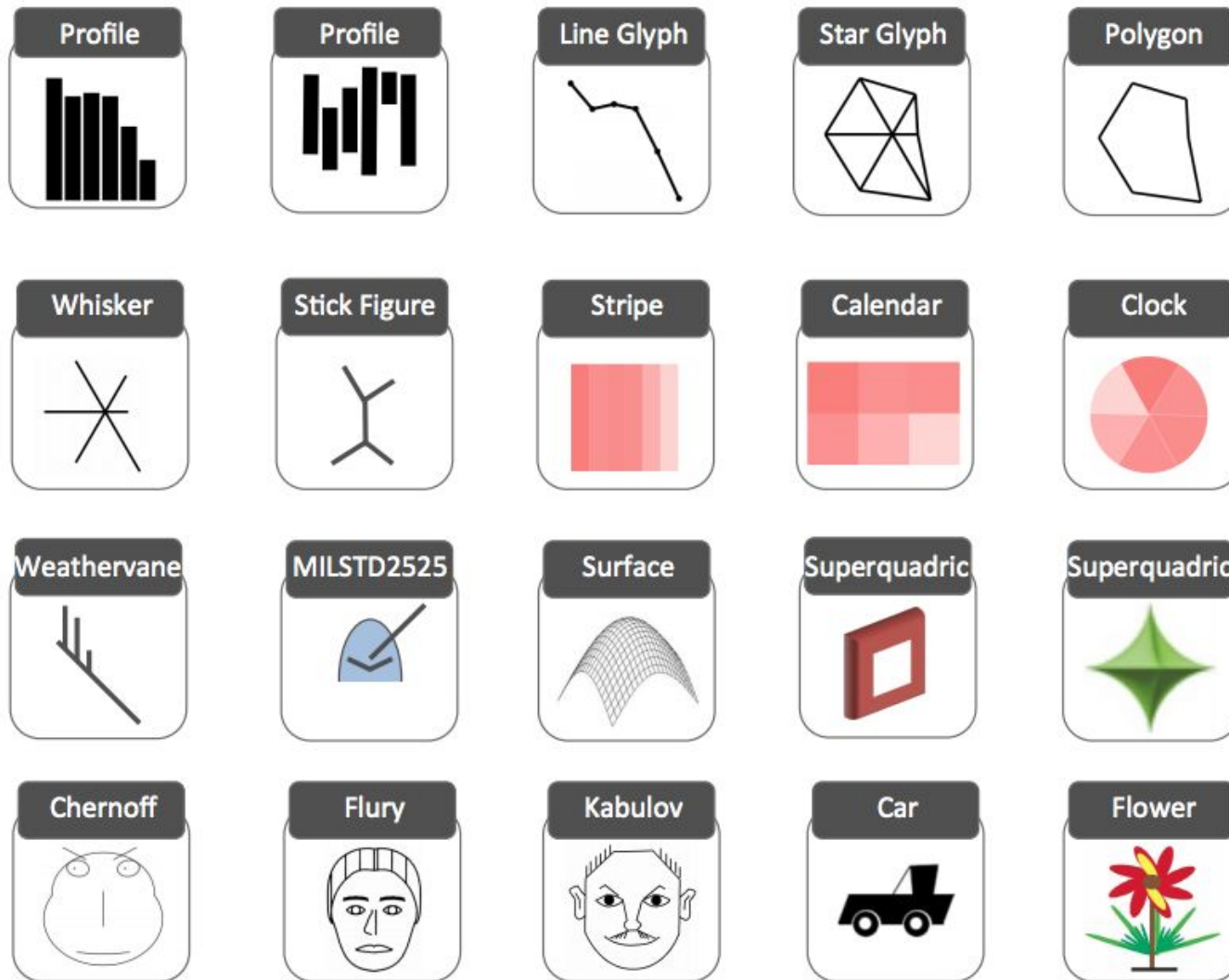


- Petals show dimensions, length shows attribute value
- Order country by values

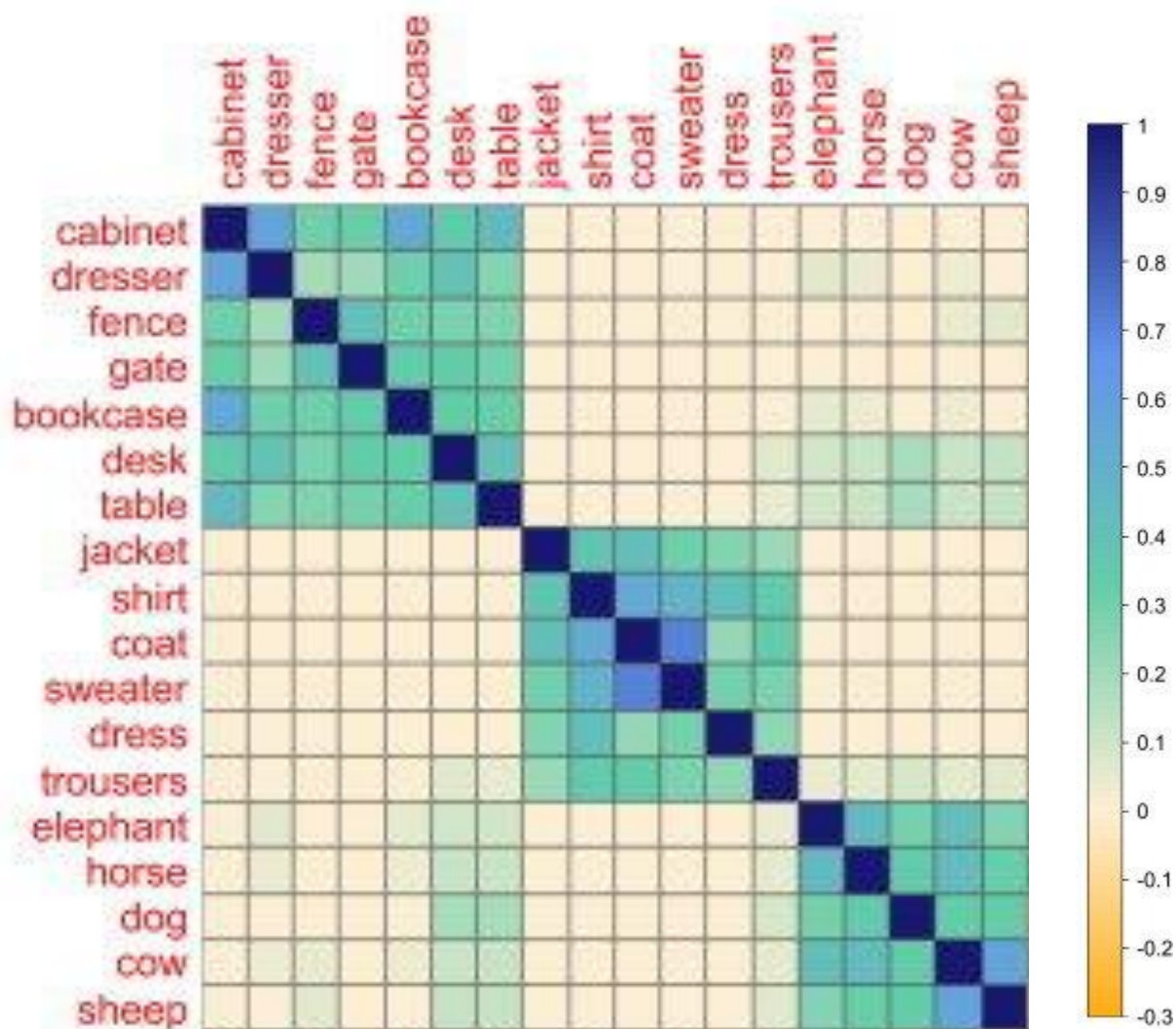
Glyphs in Scatterplots



Glyph Design



5. Dimensionality Reduction: Similarity

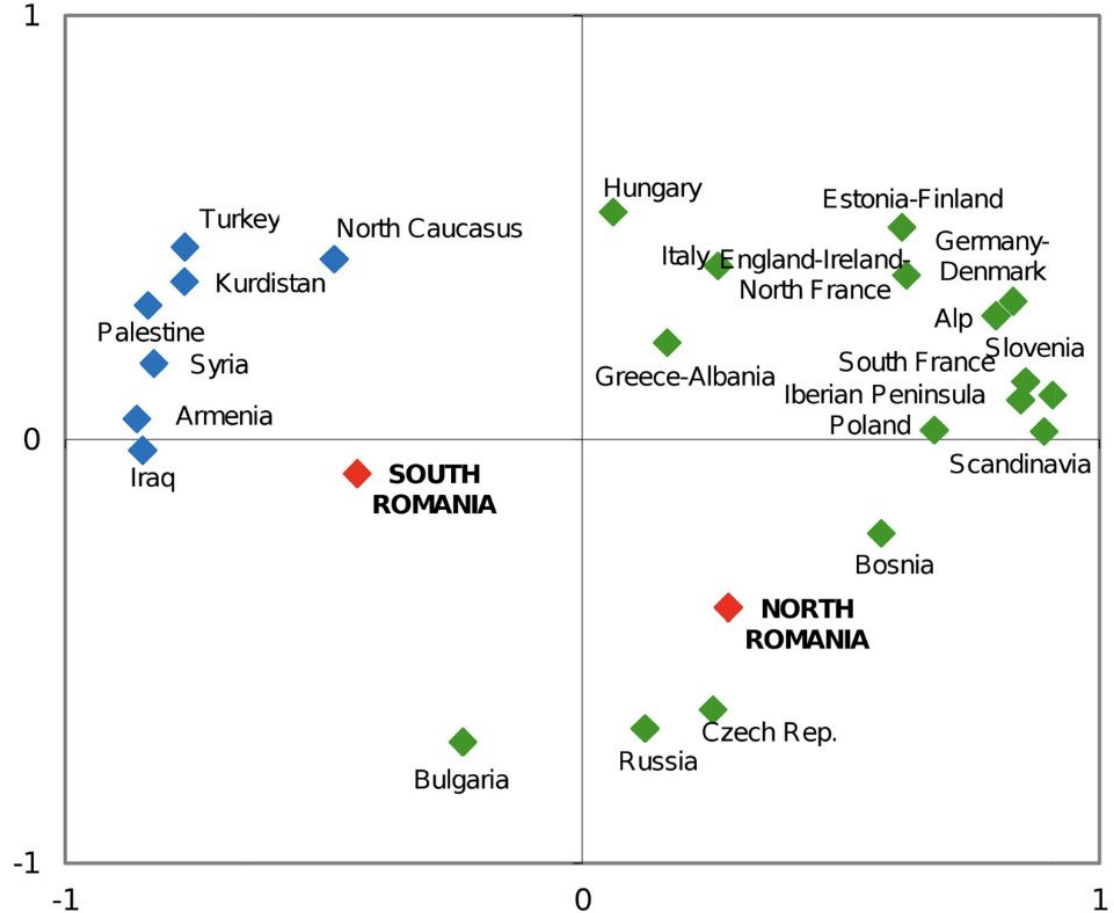


5. Dimensionality Reduction: MDS

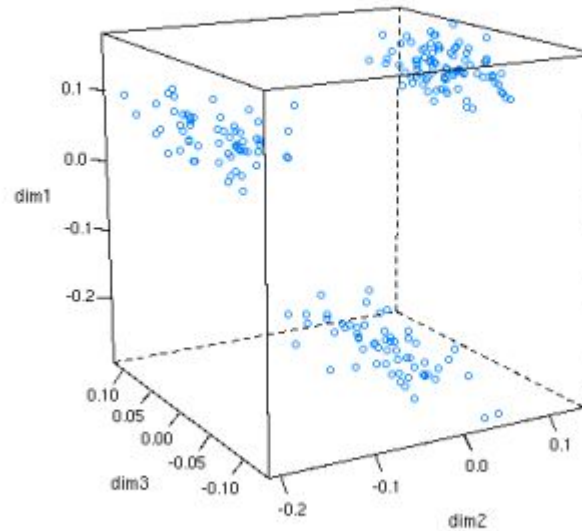
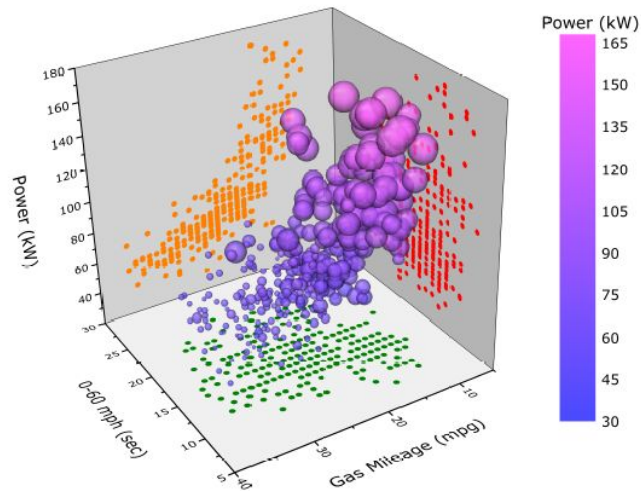


5. Dimensionality Reduction: MDS

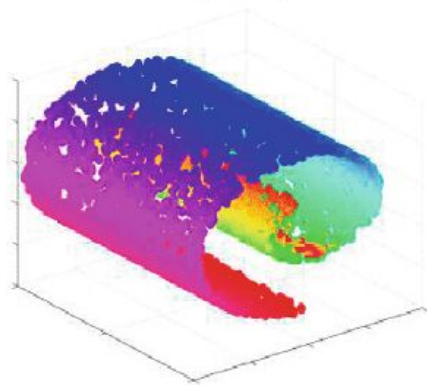
- + Dimension reduction
- + Can be 2D or 3D
- + Visual clustering
- Information loss
- Artifacts: **false neighbors** and **tears**



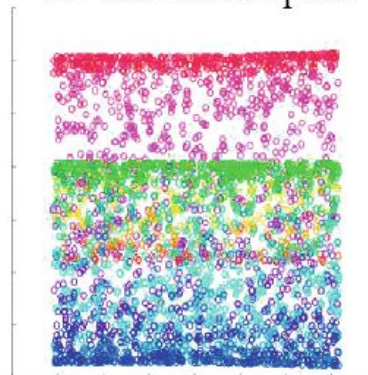
5. Dimensionality Reduction: 3D



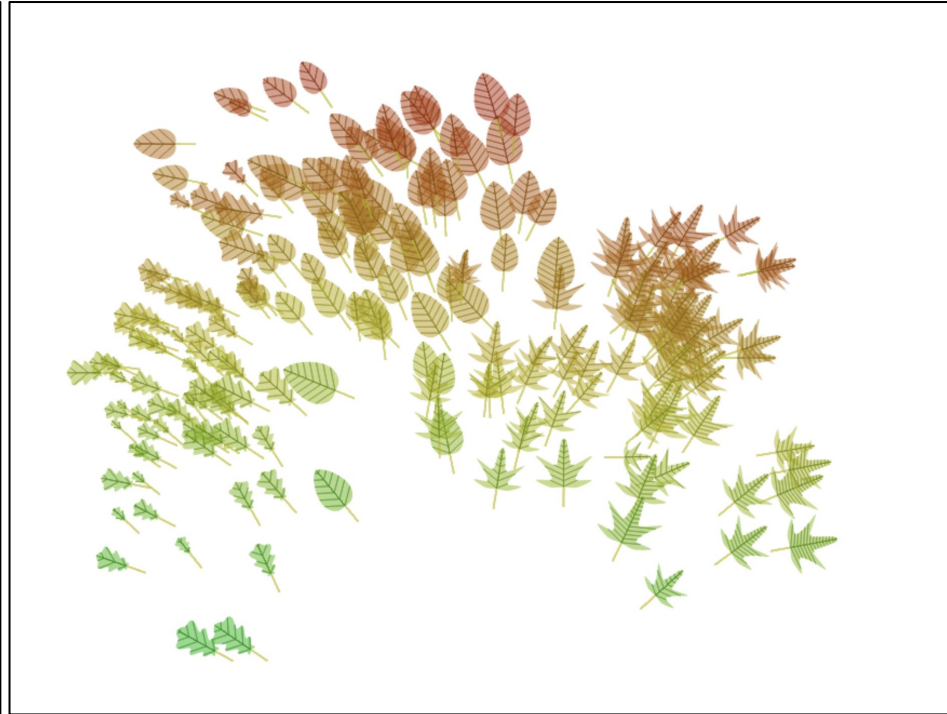
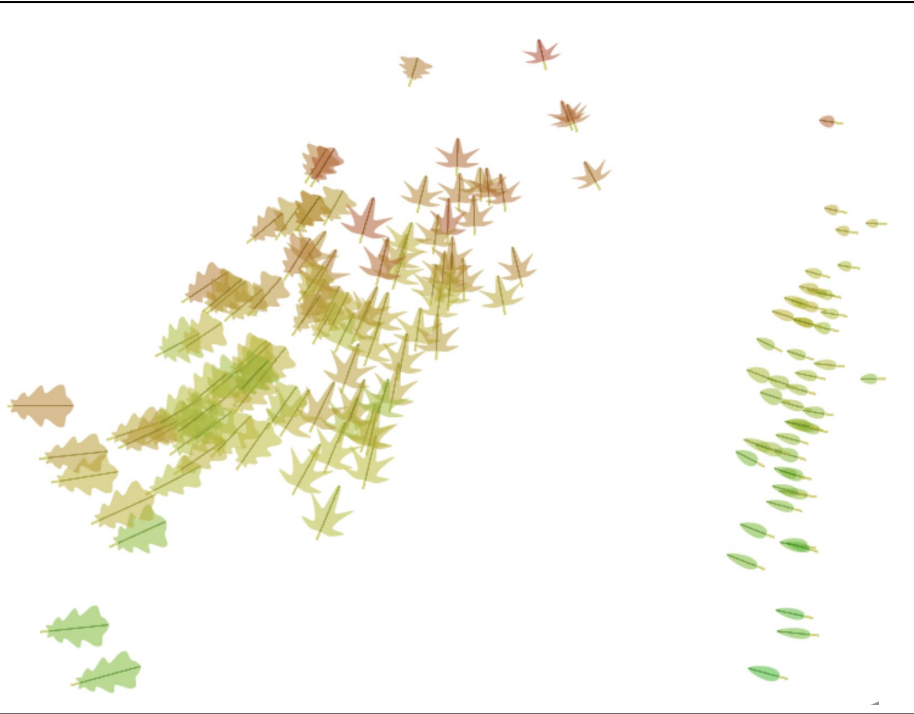
3D Input space



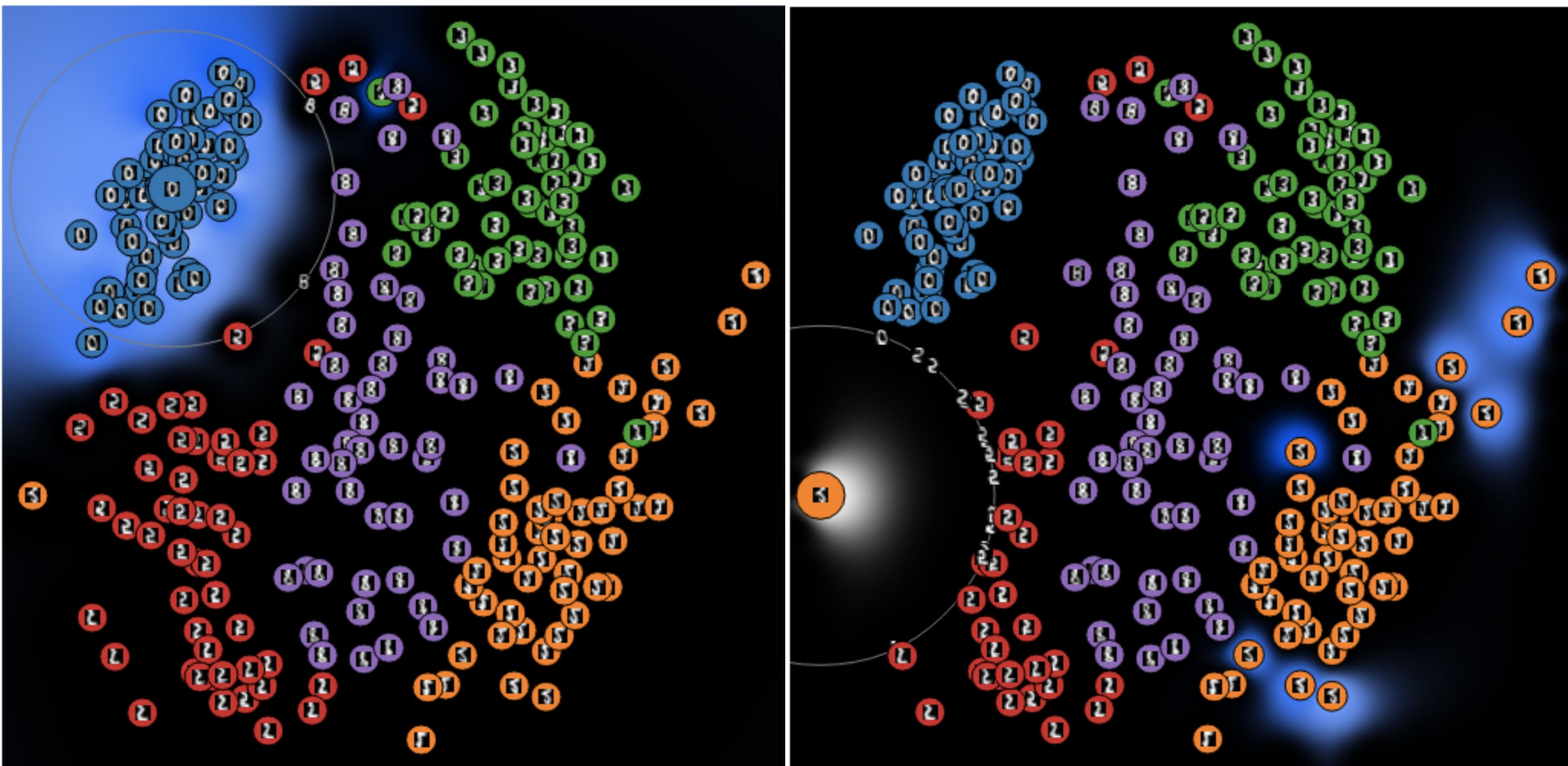
2D Embedded space



5. Dimensionality Reduction: Glyphs



5. Dimensionality reduction: Interaction



Heulot, Nicolas, Michael Aupetit, and Jean-Daniel Fekete. "Proxilens: Interactive exploration of high-dimensional data using projections." *VAMP: EuroVis Workshop on Visual Analytics using Multidimensional Projections*. The Eurographics Association, 2013.

Further Readings

- Shneiderman, Ben. "The eyes have it: A task by data type taxonomy for information visualizations." *Proceedings 1996 IEEE symposium on visual languages*. IEEE, 1996.
- Fuchs, Johannes, et al. "A systematic review of experimental studies on data glyphs." *IEEE transactions on visualization and computer graphics* 23.7 (2016): 1863–1879.
- Heinrich, Julian, and Daniel Weiskopf. "State of the Art of Parallel Coordinates." *Eurographics (STARs)*. 2013.
- <https://visualizationcheatsheets.github.io/pcp.html>